

# About **Visualization in Bergen.no** and **Interactive Visual Analysis**

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## In the Following



1. Briefly about visualization in Bergen, Norway
2. Interactive Visual Analysis (IVA)
3. High-dimensional Data IVA

HH: prof. in visualization (vis)  
 @ Dept. of Informatics (ii)  
 @ Univ. of Bergen (UiB)  
 in Bergen, Norway (.no)



UiB VisGroup

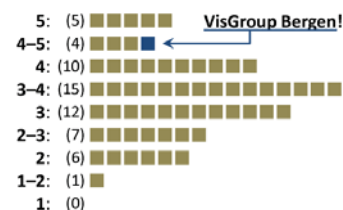
- 2007: group of 3:
- 2009: larger projects start
- 2011: EuroVis in Bergen



- 2013: new prof.:



[ranking from NFR's 10-year evaluation in 2011/2012]



ii.UiB.no/vis Research



➤ **Application-oriented basic research** in visualization:

1. Researched visualization methodology (how to visualize)

- **Interactive Visual Analysis, nD data** (H. Hauser *et al.*)
- **Visual Knowledge Discovery, 3D data** (St. Bruckner *et al.*)
- **Illustrative Visualization** (I. Viola *et al.*)

2. Applications at which this research is oriented (for whom)

- **Medical Visualization** (partner in MedViz Bergen, etc.)
- **GeoSciences / Oil & Gas** (e.g., financed by Statoil's Akademiaavtale)
- **Biology / Bioinformatics** (with CBU@ii *et al.*)
- **Fluid Dynamics** (in collab. with FFI.no, for ex.)
- **Engineering** (visual analysis of simulation data)

Area	Count
Medicine	1
Flow problems	1
GeoSciences, oil & gas	1
Biology	1
Other	1
Scientific data (in general)	1
Abstract data (in general)	1
High-dimensional problems	1
Simulation data	1
Climatology	1
Marine problems	1

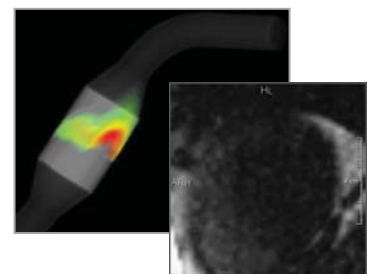


# Interactive Visual Analysis (IVA)

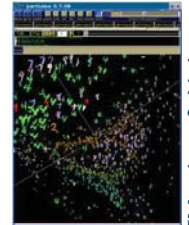
- Given data –  
*too much* and/or *too complex* to be shown at once:
- IVA is an **interactive visualization approach** to facilitate
  - the **exploration** and/or the **analysis** of data (not necessarily the presentation of data), including
    - **hypothesis generation & evaluation, sense making,**
    - **knowledge crystallization, etc.**
  - according to the **user's interest/task**, for ex., by interactive feature extraction,
  - navigating between **overview** and **details**, e.g., to enable interactive information drill-down [Shneiderman]
- through an **iterative & interactive visual dialog**

## Interactive Visual Analysis ↔ Visual Analytics

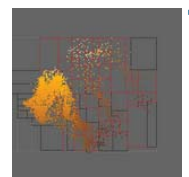
- **IVA** (“interactive visual analysis”) **since 2000**
- **Tightly related to visual analytics**, of course, e.g., *integrating computational & interactive data analysis*
- A **particular methodology** with specific components (*CMV, linking & brushing, F+C vis., etc.*)
- General enough to work in **many application fields**, but not primarily the VA fields (national security, etc.), in particular “**scientific data**” fields...



- **Goal:** to combine the *best of two worlds* [Keim et al.]:
  - data **exploration**/analysis by the **user**, based on **interactive visualization**
  - and **data analysis** by the **computer**, based on **statistics, machine learning, etc.**
- State of the art / **levels of integration**:
  - **mostly no integration**, still
  - some **vis. of results** of computations
  - also: making **comp. semi-interactive** (here called “**inner integration**”)
  - **rare: tight integration**
- **Outer integration** (here!): bundling **interaction & computation in a loop**



[Maniayar & Nabney, 2000]



[Williams & Munzner, 2004]

## Target Data Model: “Scientific Data”

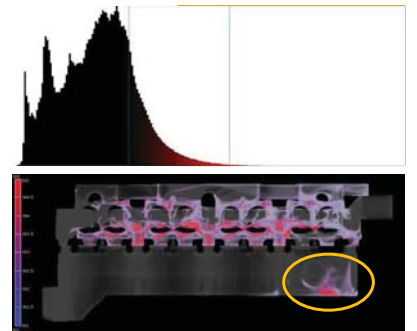
- **Characterized** by a combination of
  - **independent variables**, like **space** and/or **time** (cf. **domain**)
  - and **dependent variables**, like **pressure, temp., etc.** (cf. **range**)
- So we can think of this type of data as **given as  $d(\mathbf{x})$**  with  $\mathbf{x} \leftrightarrow$  **domain** and  $d \leftrightarrow$  **range** – examples:
  - **CT data**  $d(\mathbf{x})$  with  $\mathbf{x} \in \mathbb{R}^3$  and  $d \in \mathbb{R}$
  - **unstead 2D flow**  $\mathbf{v}(\mathbf{x}, t)$  with  $\mathbf{x} \in \mathbb{R}^2$ ,  $t \in \mathbb{R}$ , and  $\mathbf{v} \in \mathbb{R}^2$
  - **num. sim. result**  $\mathbf{d}(\mathbf{x}, t)$  with  $\mathbf{x} \in \mathbb{R}^3$ ,  $t \in \mathbb{R}$ , and  $\mathbf{d} \in \mathbb{R}^n$
  - **system sim.**  $\mathbf{q}(\mathbf{p})$  with  $\mathbf{p} \in \mathbb{R}^n$  and  $\mathbf{q} \in \mathbb{R}^m$
- **Common property**:
  - $d$  is (at least to a certain degree) **continuous** wrt.  $\mathbf{x}$



- **Interactive visual analysis** (as exemplified in this tutorial) **works really well with scientific data**, e.g.,
  - results from **numerical simulation** (spatiotemporal)
  - imaging / **measurements** (in particular multivariate)
  - sampled **models**
- When used to study scientific data, **IVA employs**
  - methods from **scientific visualization** (vol. rend., ...)
  - methods from **statistical graphics** (scatterplots, ...), **information visualization** (parallel coords., etc.)
  - **computational tools** (statistics, machine learning, ...)
- Applications include
  - **engineering, medicine, meteorology/climatology, biology, etc.**

## The Iterative Process of IVA

- Loop / bundling of *two complementary parts*:
  - **visualization** – *show to the user!*  
*Something new, or something due to interaction.*
  - **interaction** – *tell the computer!*  
*What is interesting? What to show next?*
- Basic example (**show – brush – show – ...**), cooling jacket context:
  1. show a histogram of temperatures
  2. brush high temperatures ( $>90^{\circ}[\pm 2^{\circ}]$ )
  3. show focus+context vis. in 3D
  4. locate relevant feature(s)
- **KISS-principle IVA**:
  - linking & brushing, focus+context visualization, ...

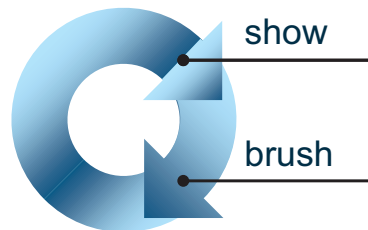


# Show & Brush

(basic IVA)

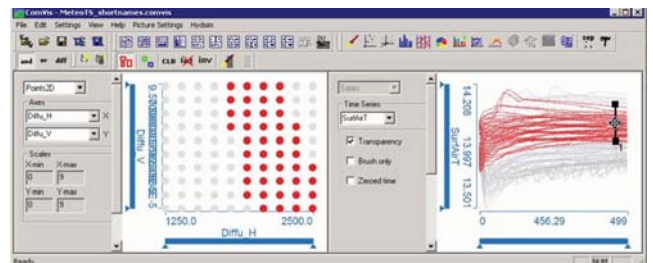


- **Tightest IVA loop**
  - **show data** (explicitly represented information)
  - **one brush** (on one view, can work on >1 dims.)



## A typical (start into an) IVA session of this kind:

- bring up multiple views
  - at least one for  $x, t$
  - at least one for  $d_i$
- I see (something)!
- brush this “something”
- linked F+C visualization
- first insight!



# Show & Brush

(basic IVA)



- **Tightest IVA loop**
  - **show data** (explicitly represented information)
  - **one brush** (on one view, can work on >1 dims.)

## Requires:

- multiple views ( $\geq 2$ )
- interactive brushing capabilities on views (brushes should be editable)
- focus+context visualization
- linking between views

## A typical (start into an) IVA session of this kind:

- bring up multiple views
  - at least one for  $x, t$
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- first insight!

... leads to ...

degree of interest

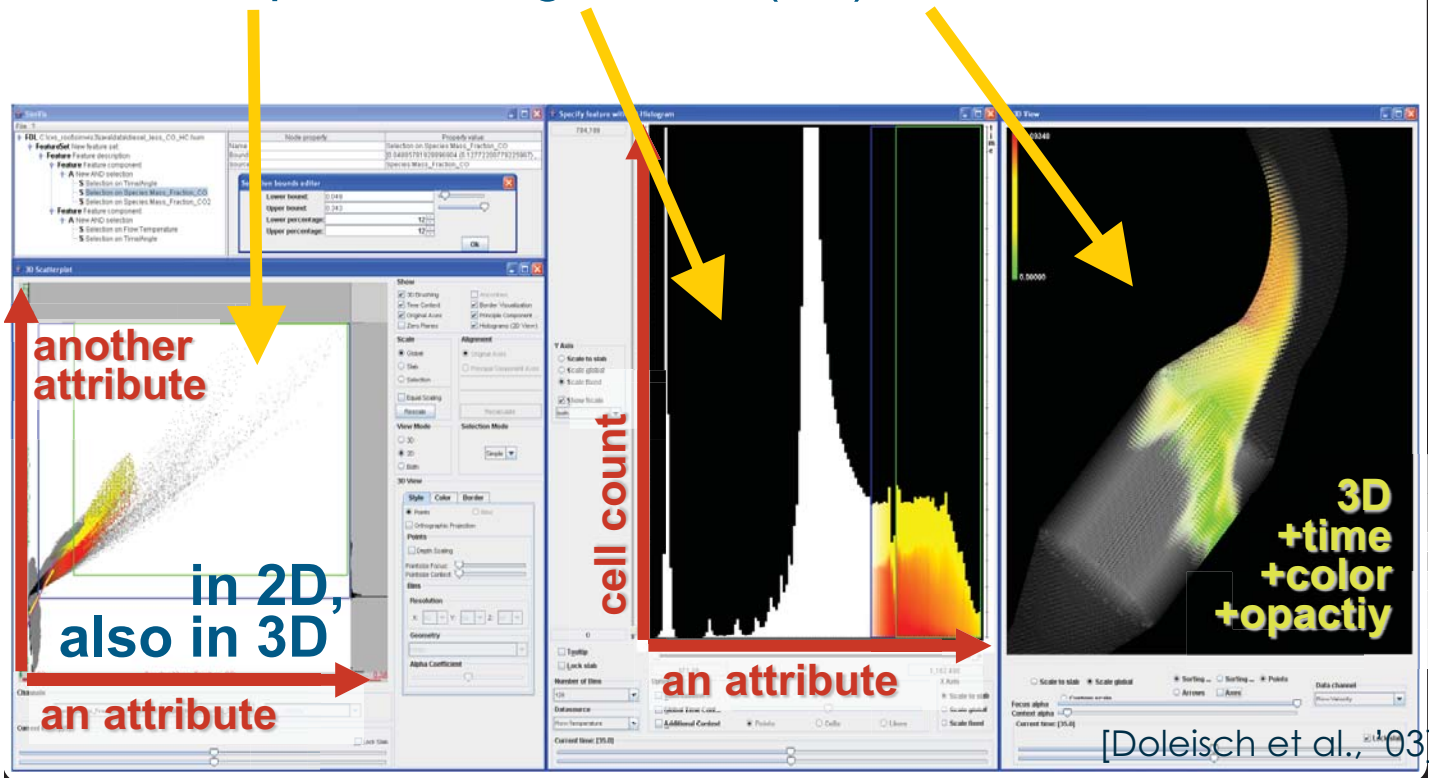
... requires ...

... is realized via ...

- Allows for **different IVA patterns** (wrt. domain & range)

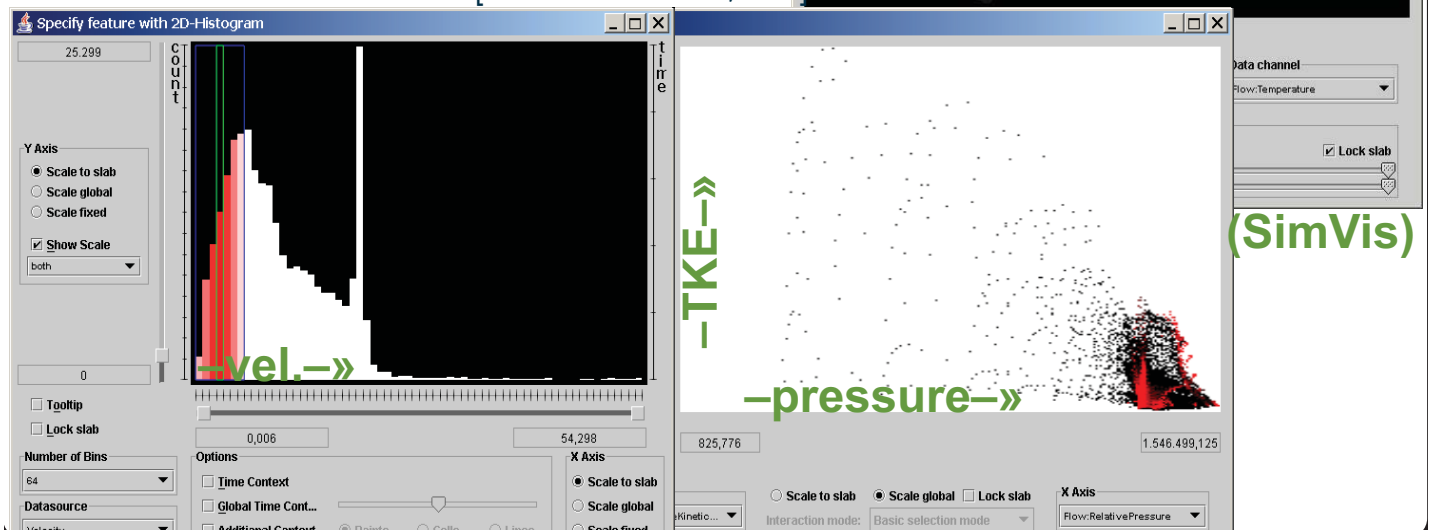
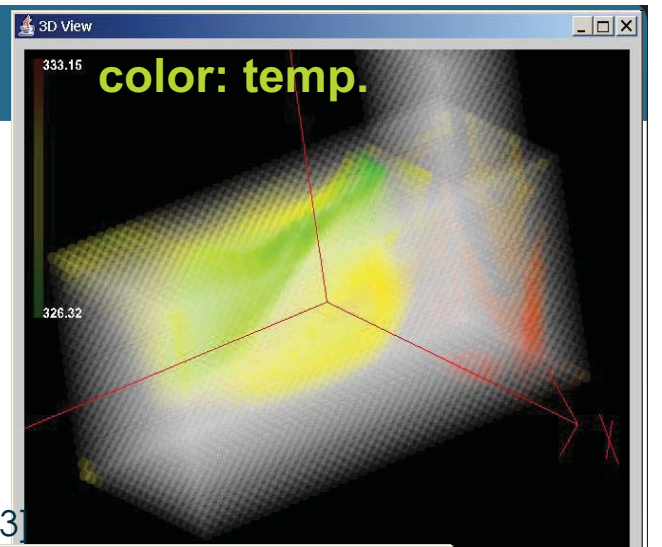
# IVA: Multiple Views

- One dataset, but multiple views
- Scatterplots, histogram, 3D(4D) view, etc.



# Interactive Brushing

- Move/alter/extend brush interactively
- Interactively explore/analyze multiple variates

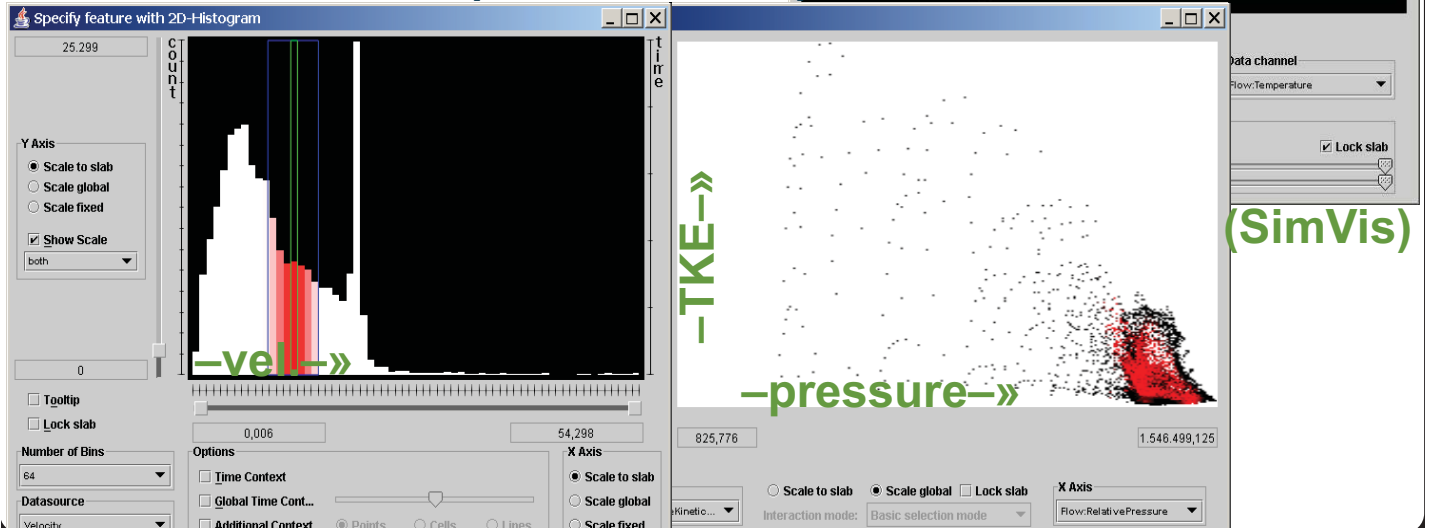
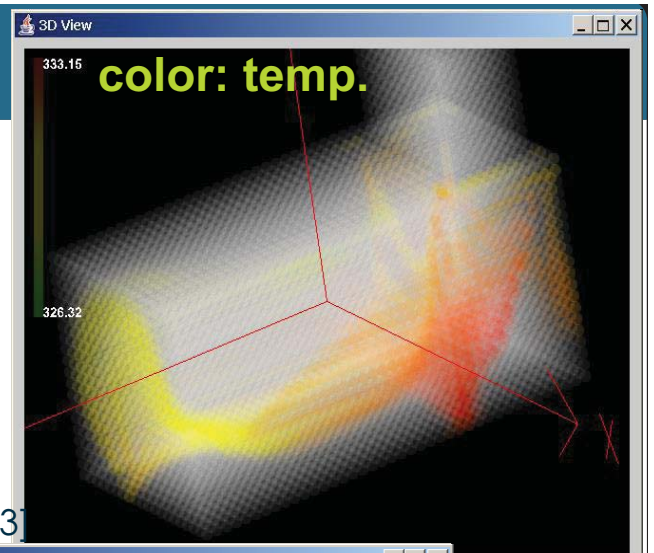




# Interactive Brushing

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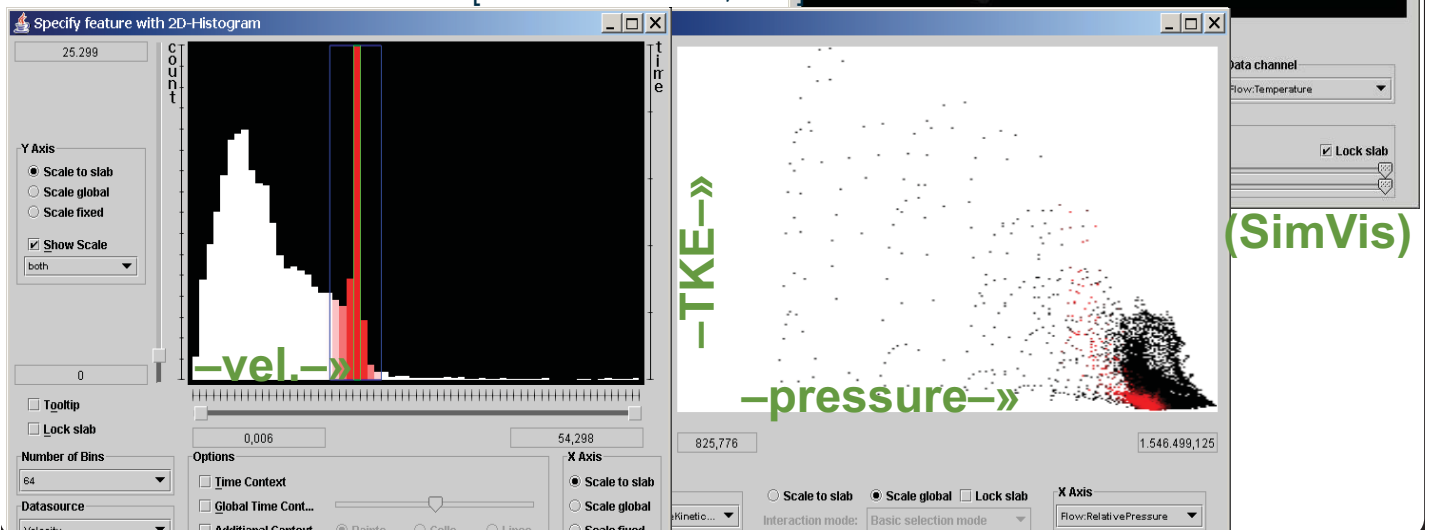
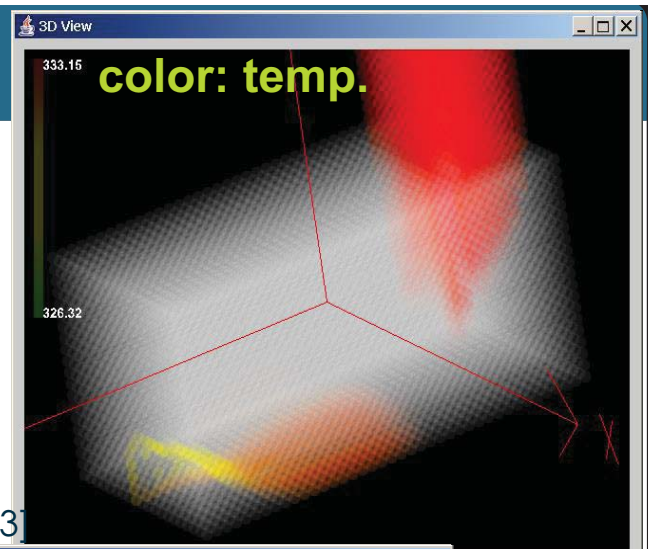
[Doleisch et al., '03]



# Interactive Brushing

- Move/alter/extend brush interactively
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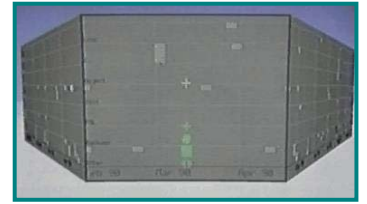
[Doleisch et al., '03]



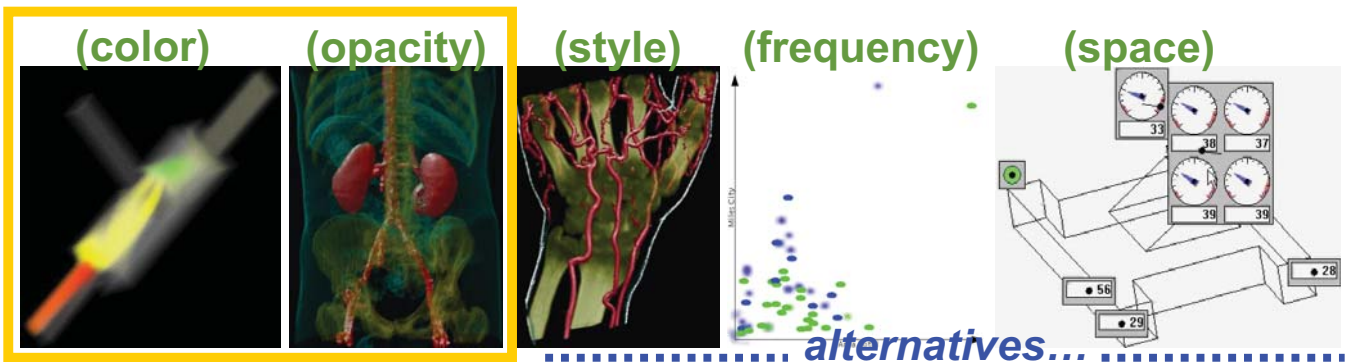
# IVA: Focus+Context Visualization

- Traditionally space distortion
  - more space for data of interest
  - rest as context for orientation
- Generalized F+C visualization
  - emphasize data in focus (color, opacity, ...)
  - differentiated use of visualization resources

[Mackinlay et al. 1991]



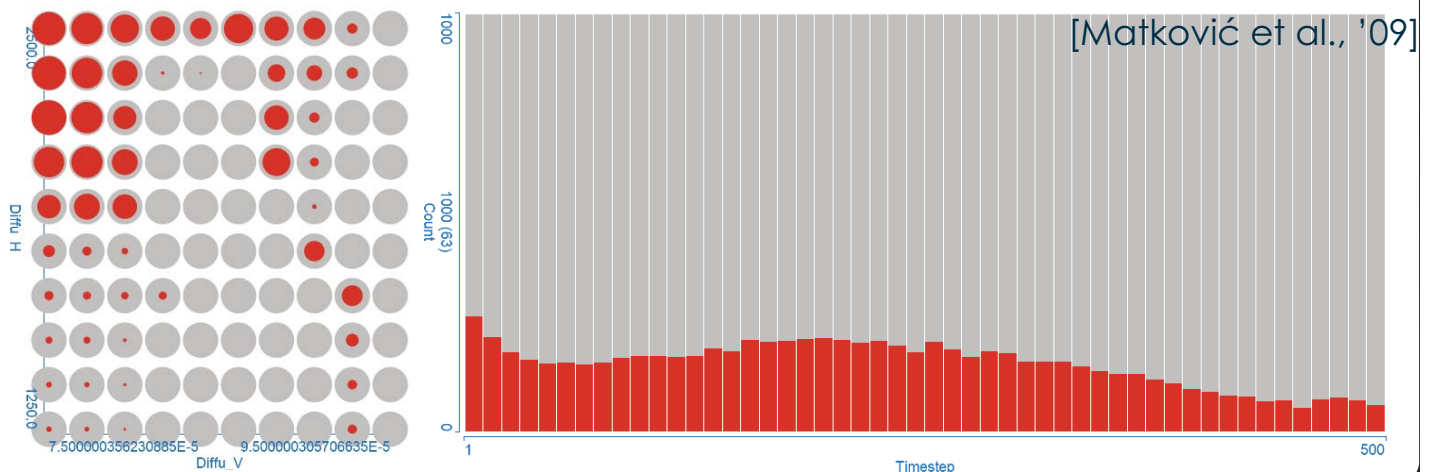
[Hauser... 2001, 2003]



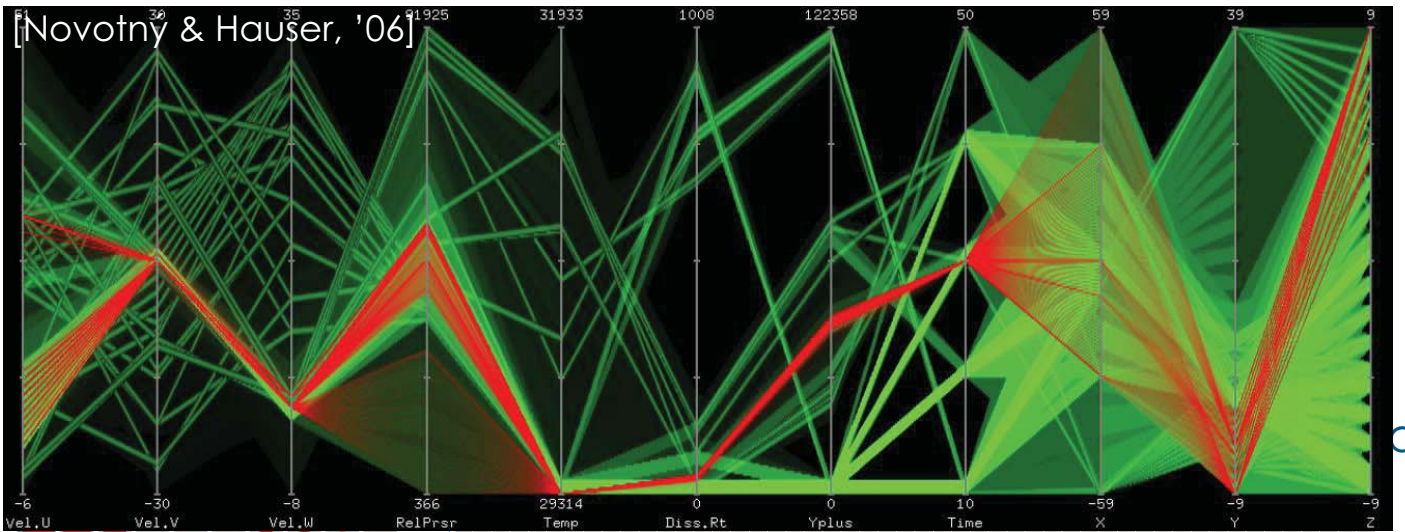
## F+C Visualization in IVA Views

- Colored vs. gray-scale visualization
- Opaque vs. semi-transparent visualization

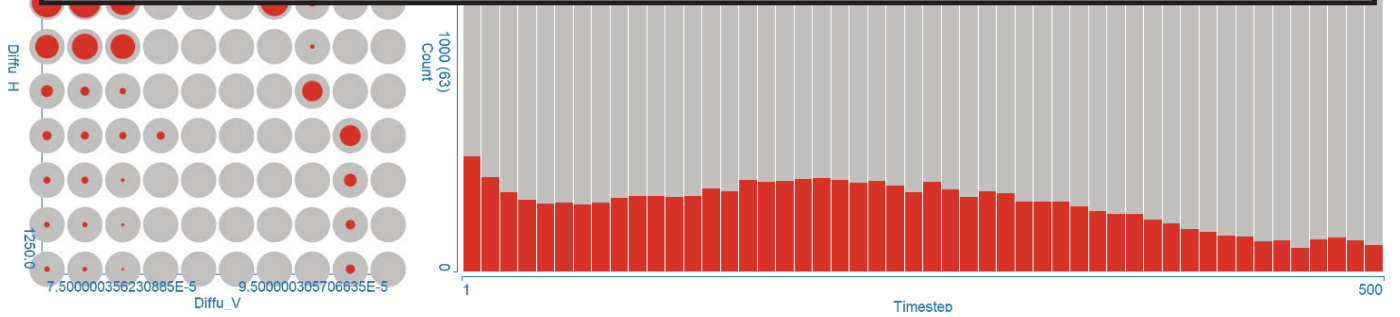
In a scatterplot (left) or histogram (right): brushed data in red



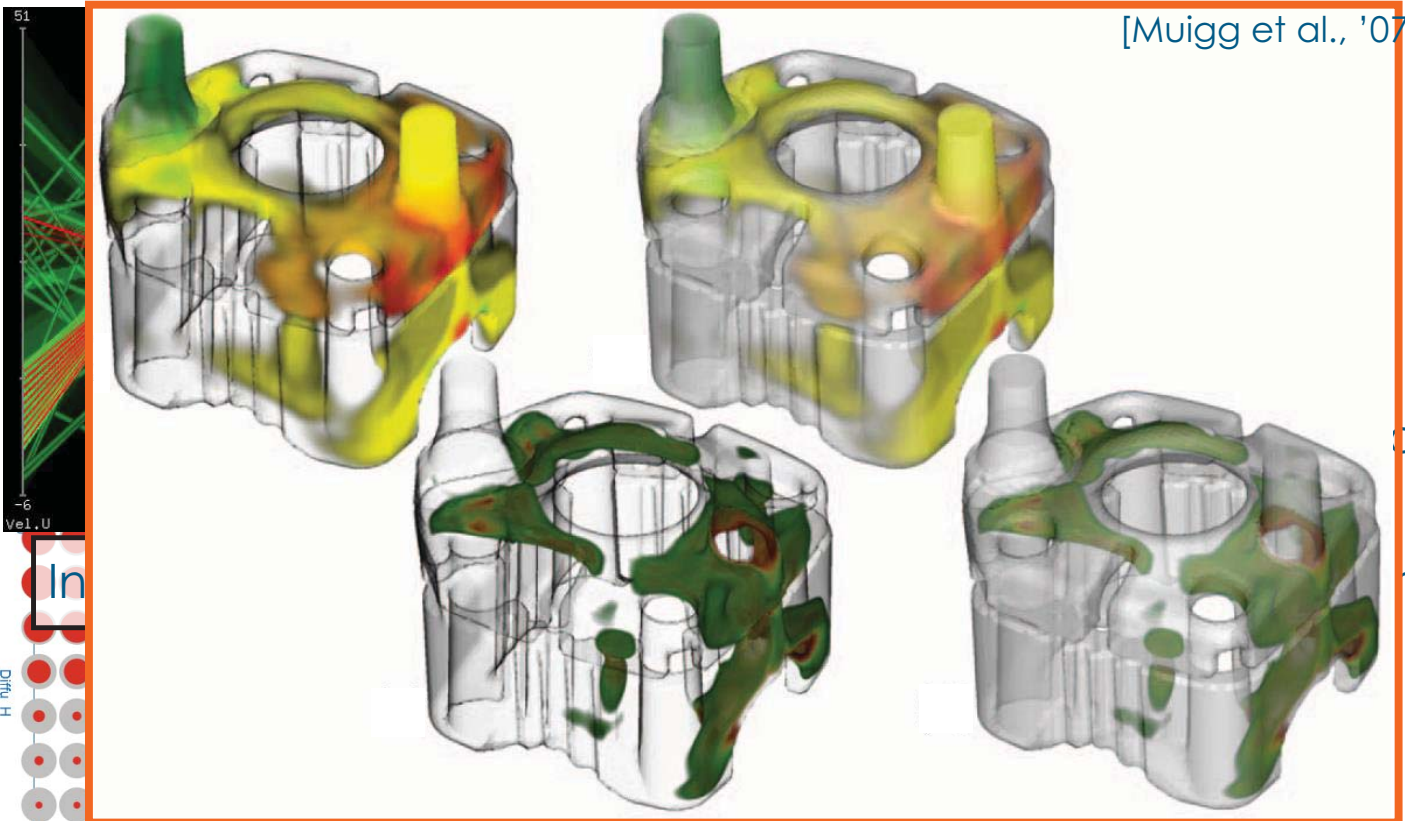
# F+C Visualization in IVA Views



In parallel coordinates (above): brushed data in red & overlaid



# F+C Visualization in IVA Views

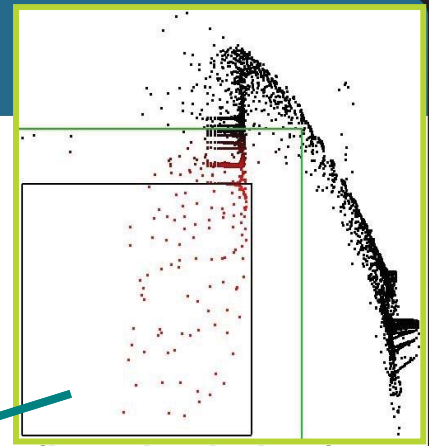


In 3D (above): less transp. & colored, in illustrative context

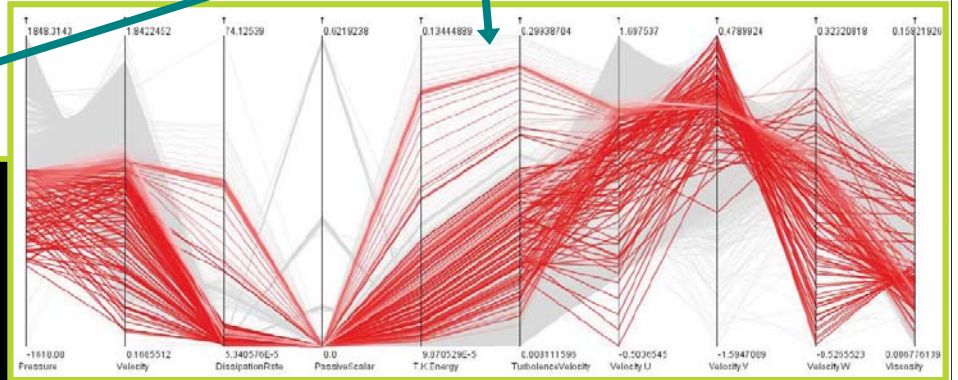


# IVA: Linked Views

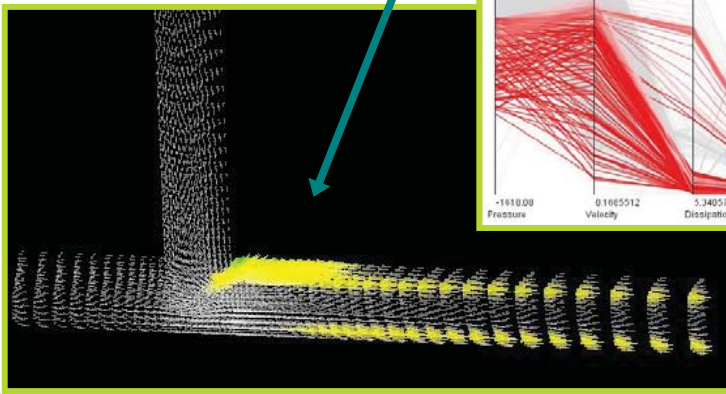
- Brushing: mark data subset as especially interesting
- Linking: enhance brushed data in linked views consistently (F+C)



(brushed view)



(linked views)



[Doleisch & Hauser, '02]

# IVA: Degree of Interest (DOI)

- $doi(.)$ : data items  $tr_i$  (table rows)  $\rightarrow$  degree of interest  
 $doi(tr_i) \in [0,1]$

- $doi(tr_i) = 0 \Rightarrow tr_i$  not interesting ( $tr_i \in$  context)
  - $doi(tr_i) = 1 \Rightarrow tr_i$  100% interesting ( $tr_i \in$  focus)

x	y	d1	d2	doi
0	0	17,20	-0,22	0,00
1	0	12,10	0,10	0,00
2	0	7,70	0,45	0,00
3	0	2,10	0,90	0,00
0	1	24,10	0,02	0,00
1	1	21,90	0,36	0,00
2	1	15,50	0,87	0,74
3	1	11,10	1,20	1,00
0	2	27,20	0,12	0,00
1	2	24,10	0,66	0,18
2	2	17,30	1,35	1,00
3	2	12,10	2,20	0,60
0	3	35,50	0,67	0,00
1	3	30,90	1,30	0,00
2	3	24,50	2,10	0,10
3	3	20,80	2,90	0,00

## Specification

- explicit, e.g., through direct selection
  - implicit, e.g., through a range slider



## Fractional DOI values: $0 \leq doi(tr_i) \leq 1$

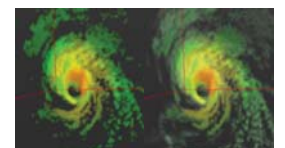
- several levels (0, low, med., ...)
  - a continuous measure of interest
  - a probabilistic definition of interest

(cont'd on next slide)

# IVA: Smooth Brushing $\rightarrow$ Fractional DOI

- Fractional DOI values** esp. useful wrt. **scientific data**:  
 (quasi-)continuous nature of data  $\leftrightarrow$  smooth borders

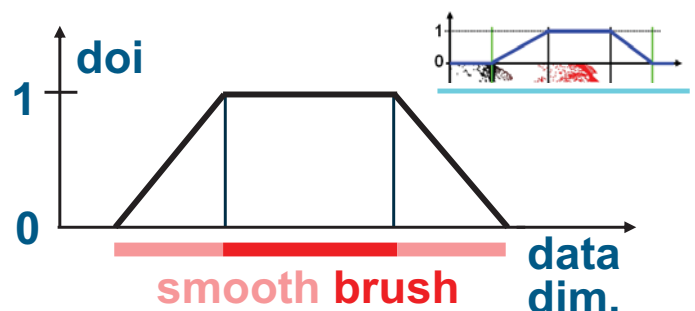
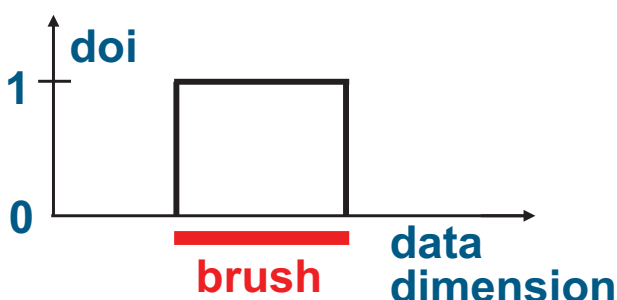
- Goes well with gradual focus+context vis. techniques (coloring, semitransparency)



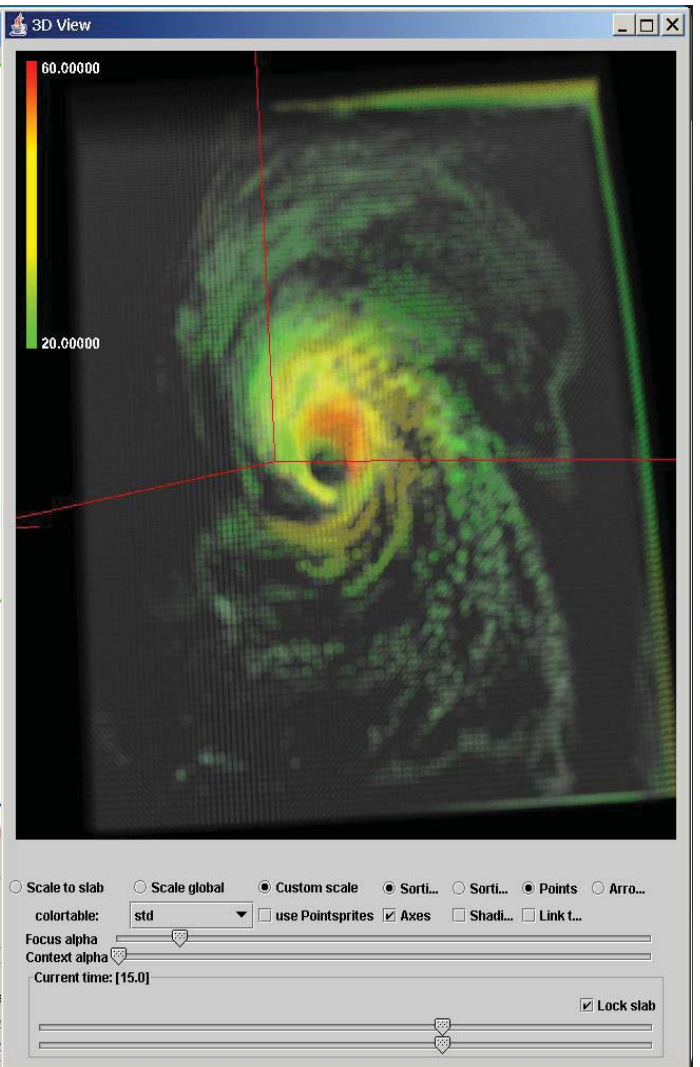
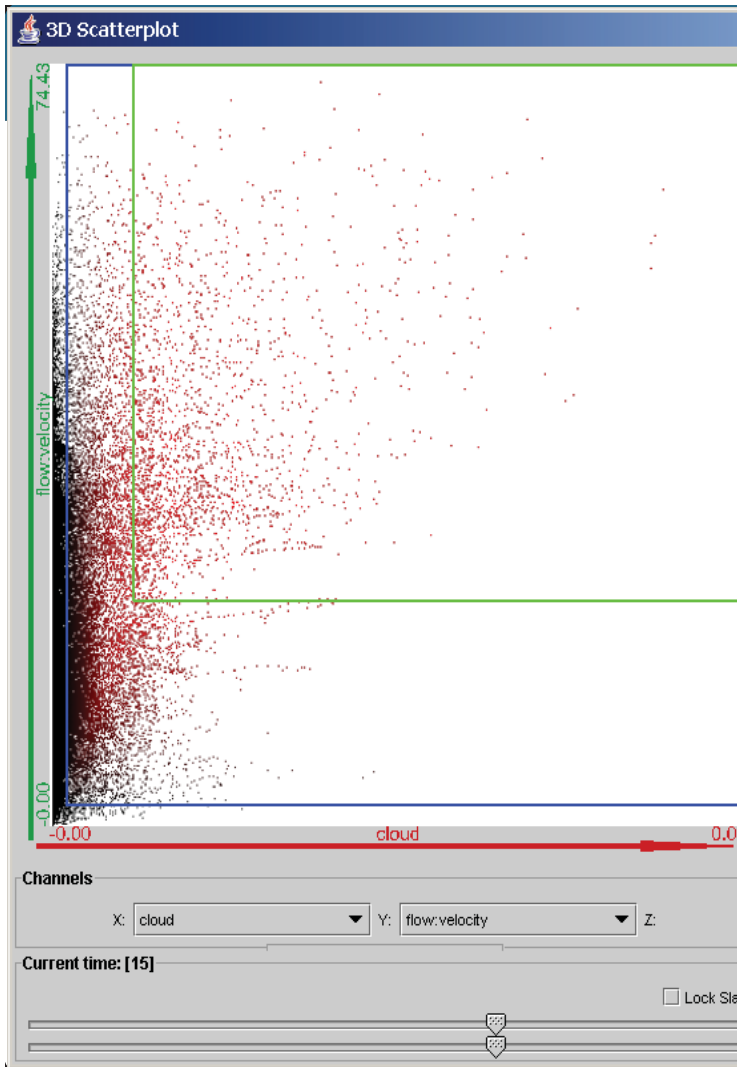
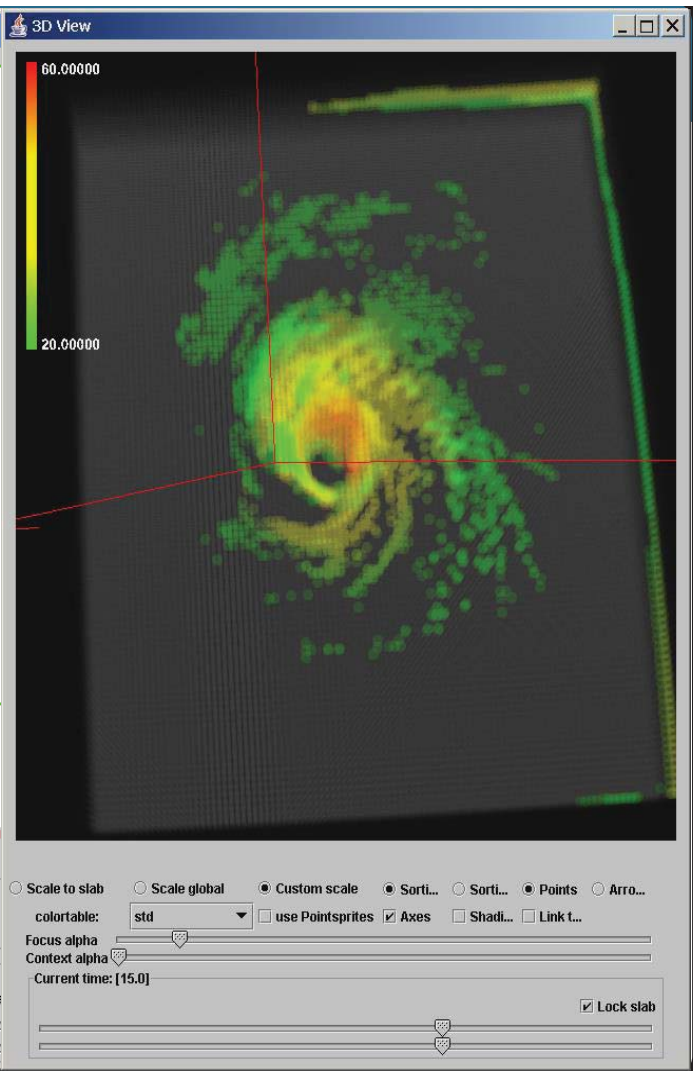
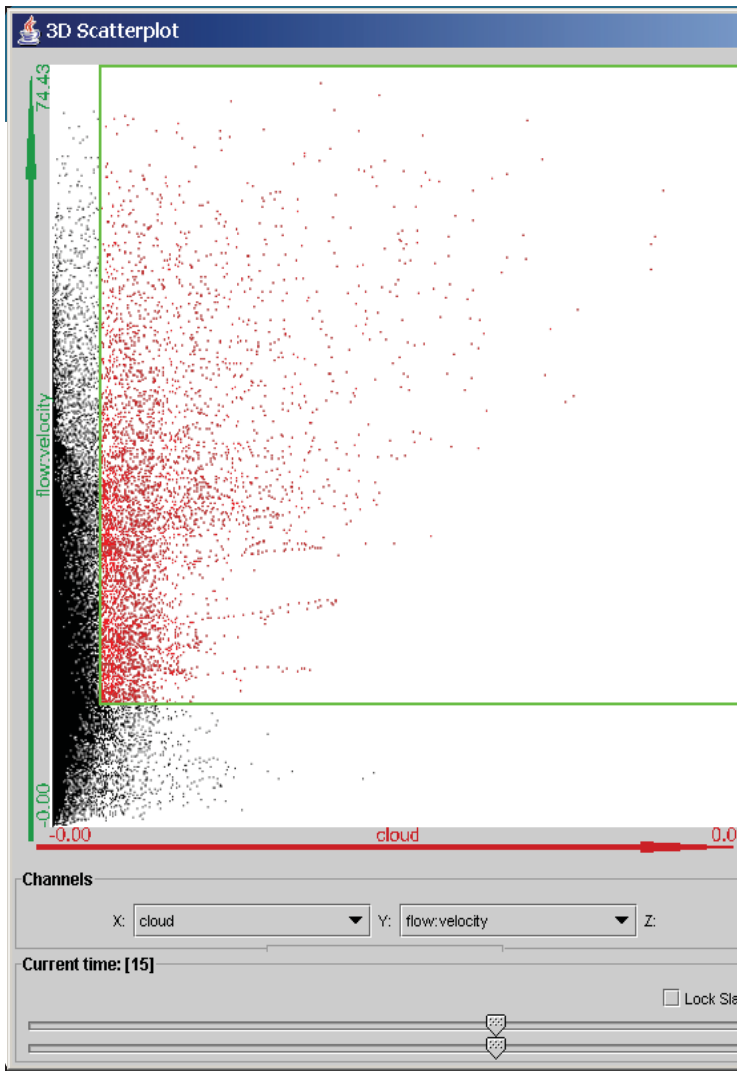
## Specification: **smooth brushing**

[Doleisch & Hauser, 2002]

- “inner” range: all 100% interesting (DOI values of 1)
  - between “inner” & “outer” range: fractional DOI values
  - outside “outer” range: not interesting (DOI values of 0)







# Three Patterns of SciData IVA

- Preliminary: domain  $x$  & range  $d$  visualized ( $\geq 2$  views)

1 ■ **brushing on domain visualization**,  
e.g., brushing special locations in the map view

▶ **local investigation** "d"

2 ■ **brushing on range visualization**,  
e.g., brushing outlier curves in a function graph view

▶ **feature localization** "x"

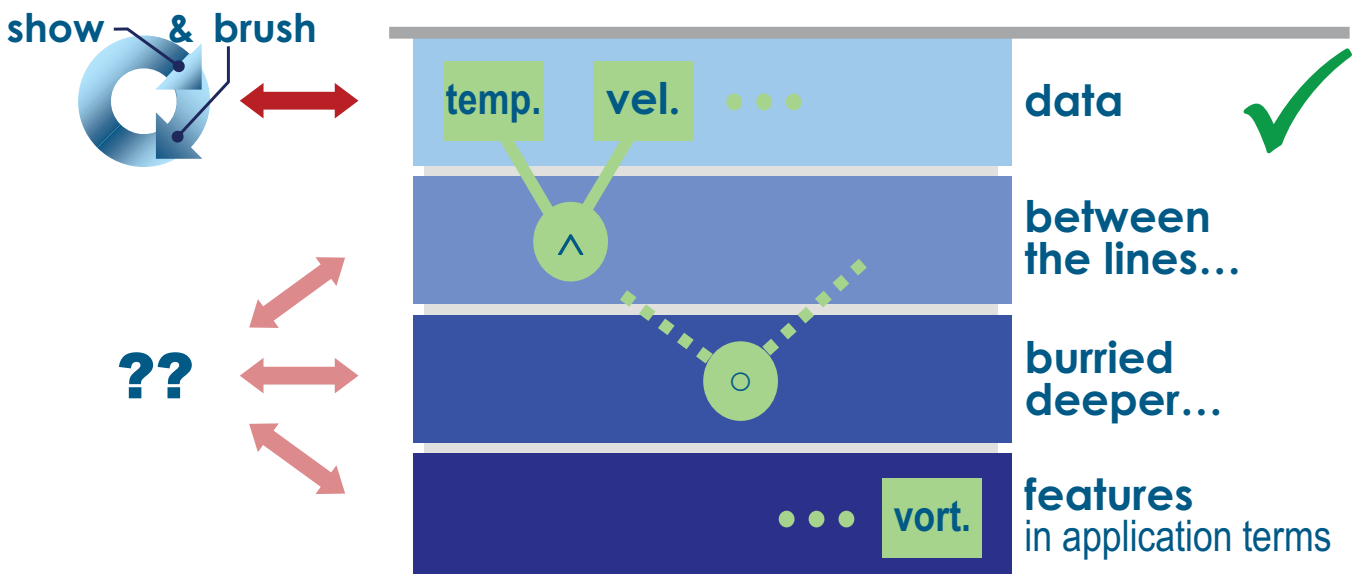
3 relating multiple range variates

▶ **multi-variate analysis** "d"

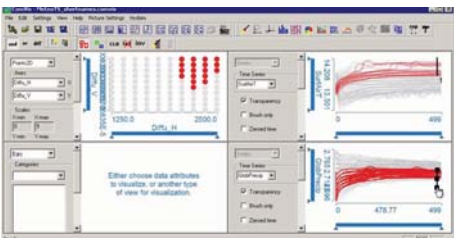
## IVA – Levels of Complexity

(1/4)

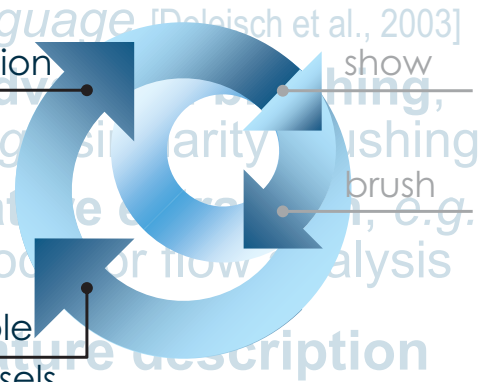
- A *lot* can be done with basic IVA, already! [pareto rule]
- We can consider a **layered information space**: from **explicitly** represented information (the **data**) to **implicitly** contained information, **features**, ...



- A *lot* can be done with basic IVA, already! ✓ [parent rule]
- For more advanced exploration/analysis tasks, we extend it (in several steps):
  - IVA, level 2: **logical combinations of brushes**, e.g., utilizing the *feature definition language* [Doleisch et al., 2003]
  - IVA, l. 3: **attribute derivation; advanced brushing**, with interactive formula editor; e.g., similarity brushing
  - IVA, l4: **application-specific feature extraction**, e.g., based on vortex extraction methods for flow analysis
- Level 2: like **advanced verbal feature description**
  - ex.: “hot flow, also slow, near boundary” (cooling j.)
  - brushes comb. with **logical operators** (AND, OR, SUB)
  - in a **tree**, or **iteratively** (((b<sub>0</sub> op<sub>1</sub> b<sub>1</sub>) op<sub>2</sub> b<sub>2</sub>) op<sub>3</sub> b<sub>3</sub>) ...)

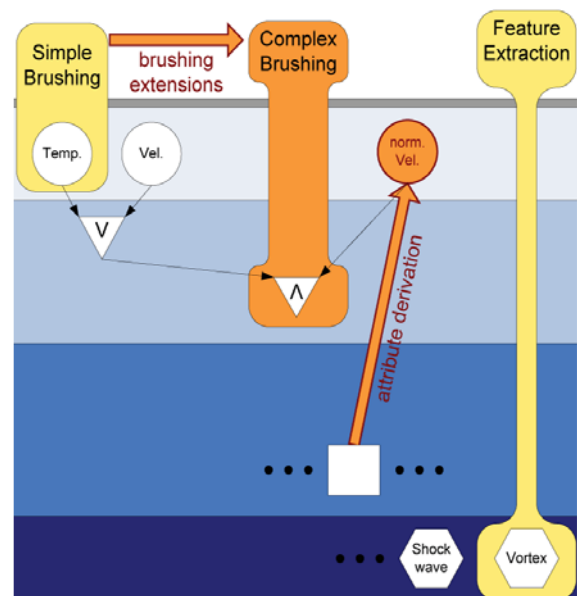


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- Level 3: using **general info extraction** mechanisms, two (partially complementary) approaches:
  1. **derive additional attribute(s)**, then show & brush
  2. use an **advanced brush** to select “hidden” relations

- A **lot** can be done with basic IVA
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- Level 3: using **general info extraction** mechanisms, two (partially complementary) approaches:
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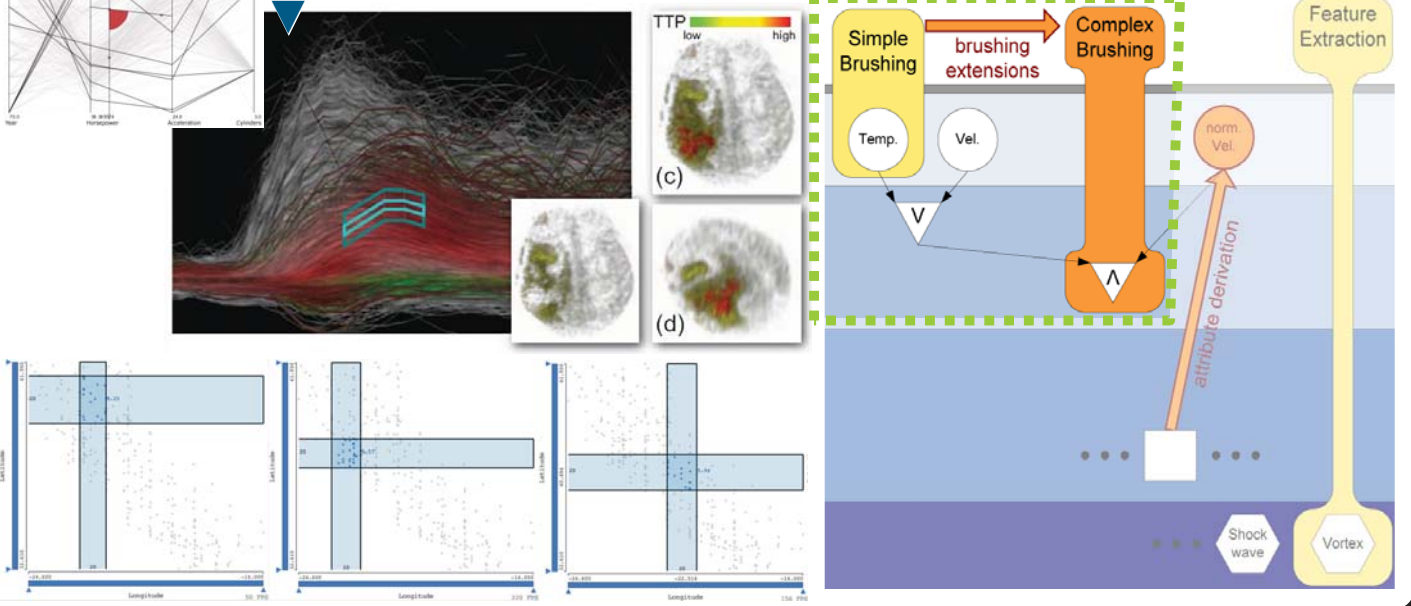


# IVA (level 3): Advanced Brushing

- **Std. brush:** brush 1:1 what you see
- **Adv. brush:** executes additional function (“intelligent?”)

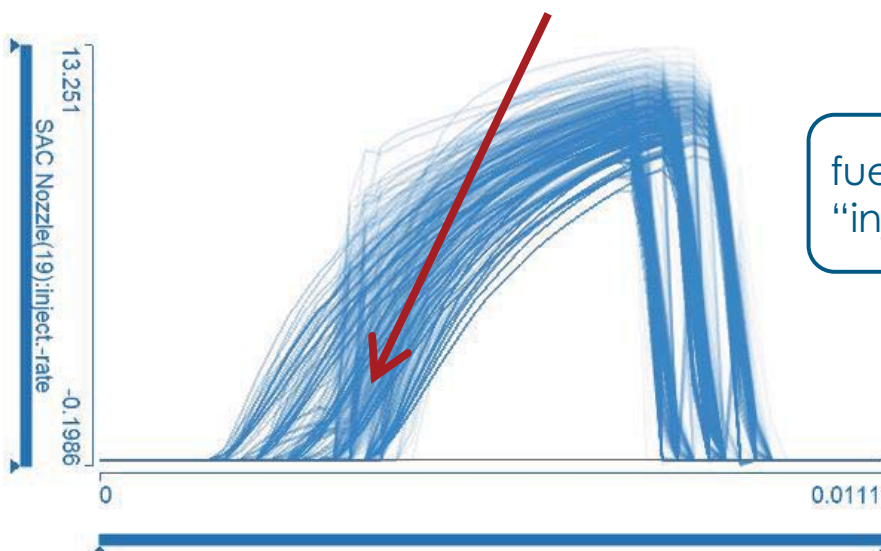
- **Examples:**

- angular brushing [Hauser et al., 2002]
  - similarity brushing [Muigg et al., 2008]



## 3<sup>rd</sup> level IVA, adv. brushing example

- Considering a visualization of a family of function graphs:
  - select the steeply rising graphs



fuel injection simulation  
“injection rate”

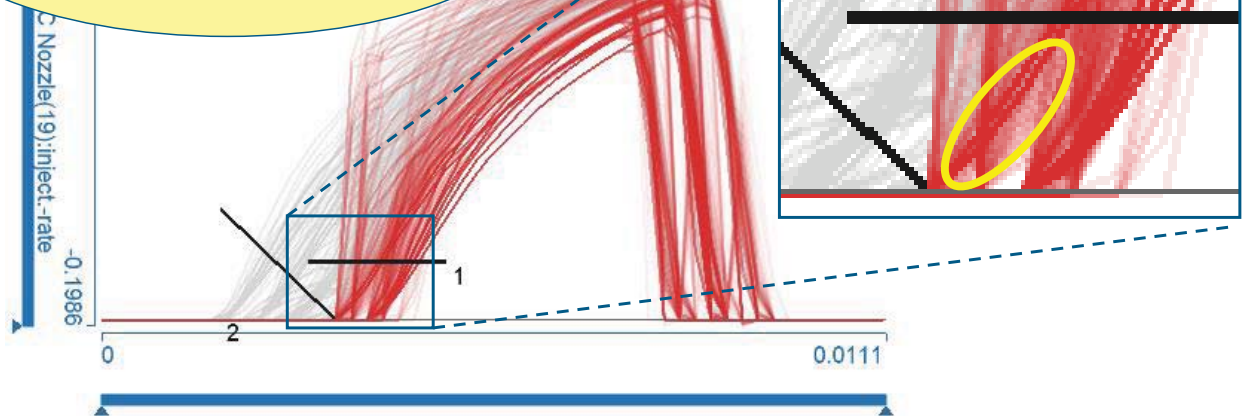


## 3<sup>rd</sup> level IVA, adv. brushing example



- A simple line brush is not enough
- Combining line brushes does not work, either

feature of interest:  
not explicitly available

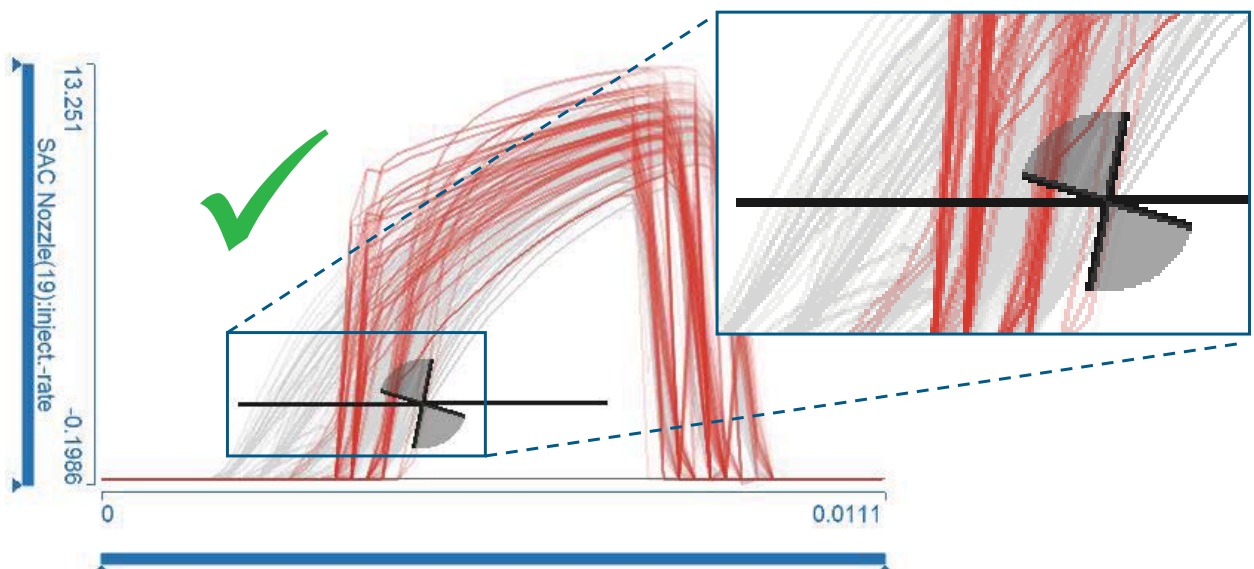


example prepared by Konyha, Zoltan

## 3<sup>rd</sup> level IVA, adv. brushing example



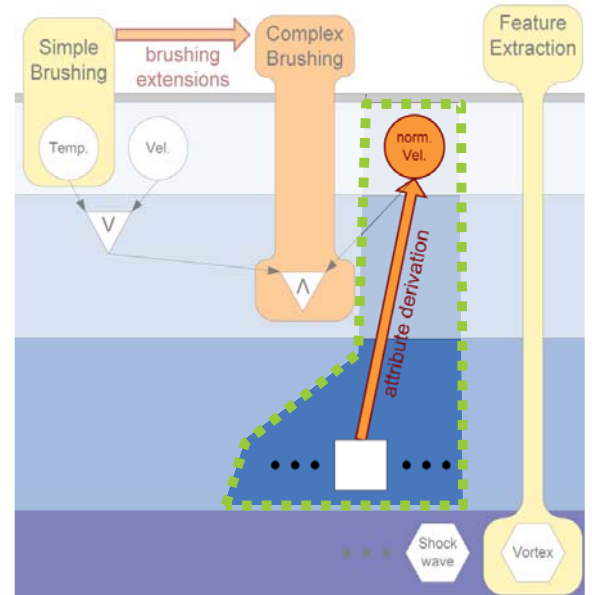
- The *angular line brush* (a specialized brush) selects the intended function graphs
  - that it intersects, and
  - the angle is in a given threshold



example prepared by Konyha, Zoltan

# IVA (level 3): Attribute Derivation

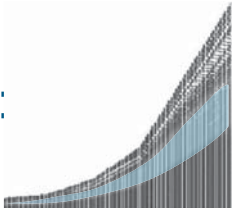
- **Principle** (in the context of iterative IVA):
  - see some data feature  $\Phi$  of interest in a visualization
  - identify a **mechanism T** to describe  $\Phi$
  - **execute** (interactively!) an **attribute derivation** step to represent  $\Phi$  explicitly (as new, synthetic attribute[s]  $d_\phi$ )
  - brush  $d_\phi$  to get  $\Phi$
- **Tools T** to describe  $\Phi$  from:
  - numerical mathematics
  - statistics, data mining
  - *etc.*
  - **scientific computing**
- **IVA w/ T  $\leftrightarrow$  visual computing**

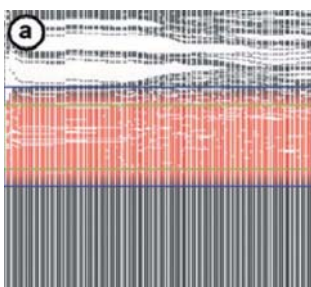


## Attribute Derivation $\leftrightarrow$ User Task / example

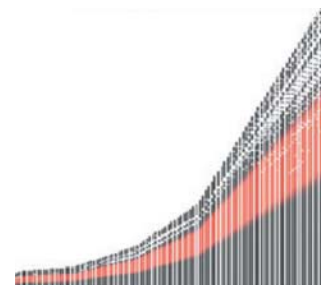
- The tools T, available in an IVA system, must reflect/match the **analytical steps of the user**:

### ■ Example:

- **first vis.:**   $\leftrightarrow$  user wishes to select the “band” in the middle
- **so?** an advanced brush? a lasso maybe?
- **ah!**  $\rightarrow$  let's normalize y and then brush (a)



- **leading to the wished selection:**



## What user wishes to reflect?

- Many **generic wishes** – users interest in:
  - something **relative** (instead of some absolute values),  
example: show me the *top-15%*
  - **change** (instead of current values),  
ex.: show me *regions with increasing temperature*
  - some **non-local property**,  
ex.: show me regions with *high average temperature*
  - **statistical properties**,  
ex.: show me *outliers*
  - **ratios/differences**,  
ex.: show me population per area, difference from trend
  - *etc.*
- **Common characteristic here:**
  - **questions/tools generic**, not application-dependent!

## How to reflect these user wishes?

- Many **generic wishes** – users interest in:
  - something **relative** (instead of some absolute values),  
example: show me the *top-15%* ⇒ **use, e.g., normalization**
  - **change** (instead of current values),  
ex.: show me *regions with increasing temperature* ⇒ **derivative estimation**
  - some **non-local property**,  
ex.: show me regions with *high average temperature* ⇒ **numerical integration**
  - **statistical properties**,  
ex.: show me *outliers* ⇒ **descriptive statistics**
  - **ratios/differences**,  
ex.: show me population per area, difference from trend ⇒ **calculus**
  - *etc.* ⇒ **data mining**  
(fast enough?)
- **Common characteristic here:**
  - **questions/tools generic**, not application-dependent!

- From **analysis, calculus, num. math**:
  - **linear filtering** (convolve the data with some linear filter on demand, e.g., to smooth, for derivative estimation, etc.)
  - **calculus** (use an interactive formula editor for computing simple relations between data attributes; +, -, ·, /, etc.)
  - **gradient estimation, numerical integration** (e.g., wrt. space and/or time) ⇒ example
  - **fitting/resampling** via **interpolation/approximation**
- From **statistics, data mining**:
  - **descriptive statistics** (compute the statistical moments, also robust, measures of outlyingness, detrending, etc.) ⇒ example
  - **embedding** (project into a lower-dim. space, e.g., with PCA for a subset of the attribs., etc.) ⇒ example
- **Important**: executed on demand, after prev. vis.

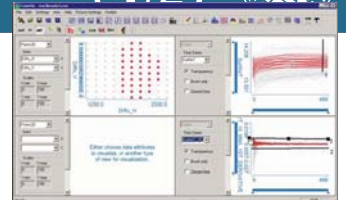
## 3<sup>rd</sup>-level IVA – Sample Iterations

(1/2)

### ■ The Iterative Process of 3<sup>rd</sup>-level IVA:

#### ■ Example 1:

- you look at some *temp. distribution over some region*
- you are *interested in raising temperatures, but not temperature fluctuations*
- you use a **temporal derivate estimator**, for ex., central differences  $t_{\text{change}} = (t_{\text{future}} - t_{\text{past}}) / \text{len}(\text{future-past})$
- you plot  $t_{\text{change}}$ , e.g., in a **histogram** and **brush** whatever change you are interested in
- maybe you see some frequency amplification due to derivation, **so you go back** and
- **use an appropriate smoothing filter** to *remove high frequencies from the temp. data*, leading to a derived new  $\tau = t_{\text{smooth}}$  data attribute
- selecting from a **histogram** of  $\tau_{\text{change}}$  (computed like above) is then less sensitive to temperature fluctuations

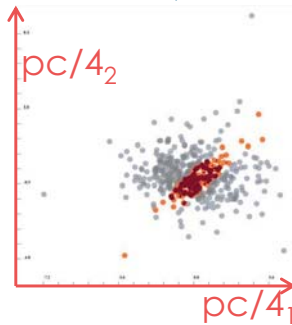
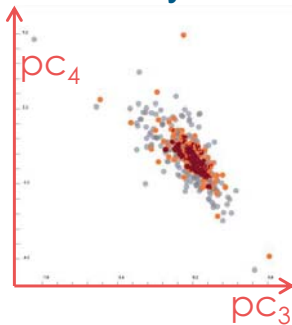
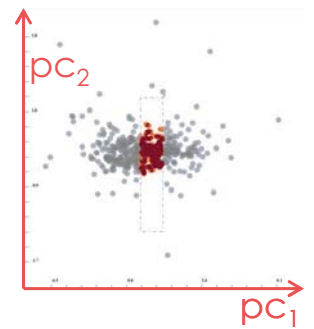
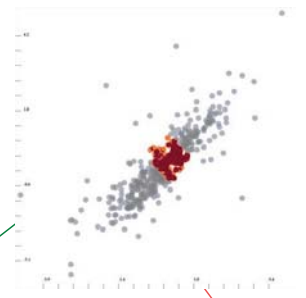




## ■ The Iterative Process of 3<sup>rd</sup>-level IVA:

### ■ Example exploiting PCA:

- you bring up a scatterplot of  $d_1$  vs.  $d_2$ :  
(from an ECG dataset [Frank, Asuncion; 2010])
- obviously,  $d_1$  and  $d_2$  are correlated, our interest: the **data center** wrt. the **main trend**
- we ask for a (local) **PCA** of  $d_1$  and  $d_2$ :
- then we **brush the data center**
- we get the wished selection
- from here further steps are possible..., incl. study of other PCA-results, etc.



[IEEE Vis, 2008]

## Brushing of Attribute Clouds for the Visualization of Multivariate Data

Heike Jänicke, Michael Böttinger, and Gerik Scheuermann, *Member, IEEE*

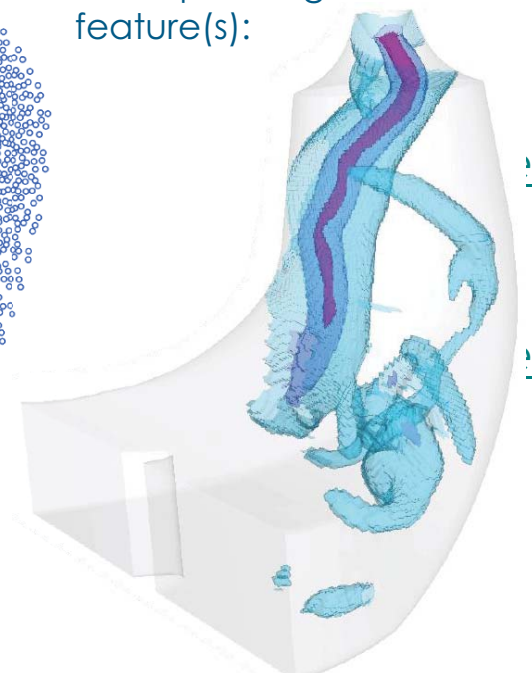
2D embedding:  
the attribute cloud



brushed  
cloud:

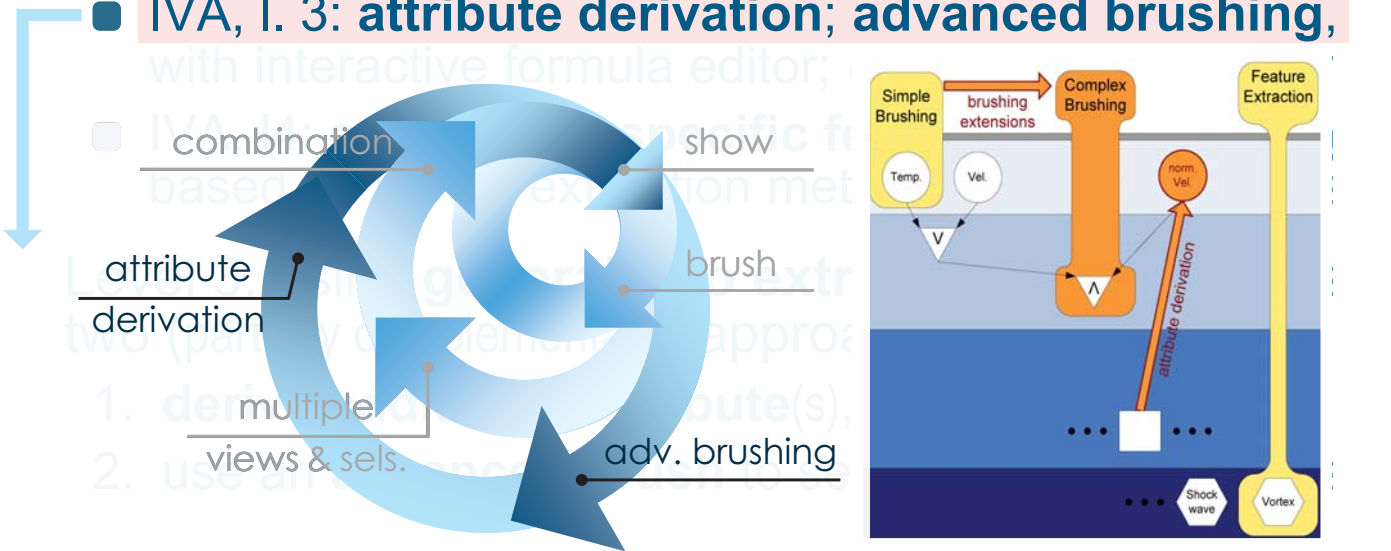


corresponding  
feature(s):





- A **lot** can be done with basic IVA, already! ✓ [parent rule]
- For more advanced exploration/analysis tasks, we extend it (in several steps):
  - IVA, level 2: **logical combinations of brushes** utilizing the *feature definition language* [Dreisch et al., 2009]
  - IVA, l. 3: **attribute derivation; advanced brushing**,

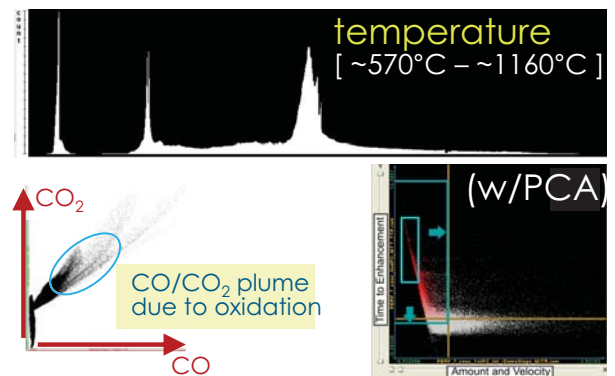


- A **lot** can be done with basic IVA, already! ✓ [parent rule]
- For more advanced exploration/analysis tasks, we extend it (in several steps):
  - IVA, level 2: **logical combinations of brushes** utilizing the *feature definition language* [Dreisch et al., 2009]
  - IVA, l. 3: **attribute derivation; advanced brushing**, with interactive formula editor; e.g., similarity
  - IVA, l4: **application-specific feature extraction**, based on vortex extraction methods for flow analysis

- Level 4: **application-specific procedures**
  - tailored solutions (for a specific problem)
  - “deep” information drill-down
  - *etc.*

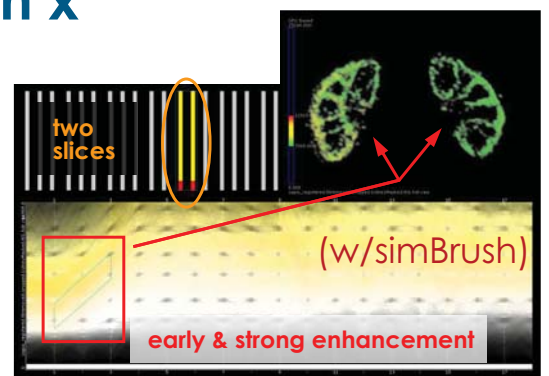
## Understanding data wrt. range $d$

- which distribution has data attribute  $d_i$ ?
- how do  $d_i$  and  $d_j$  relate to each other? (**multivariate analysis**)
- which  $d_k$  discriminate data features?



## Understanding data wrt. domain $x$

- where** are relevant features? (**feature localization**)
- which** values at specific  $x$ ? (**local analysis**)
- how are they **related to parameters**?



# The Iterative Process of IVA...

- ...is a **very useful methodology** for **data exploration & analysis**
- ...is **very general** and can be (has already been) applied to **many different application fields** (in this talk the focus was on scientific data)
- ...**meets scientific computing** as a complementary methodology (with the **important difference** that in IVA the **user** with his/her **perception/cognition** is **in the loop** at **different frequencies**, also many fps)
- ...is **not yet fully implemented** (we've done something, e.g., in the context of **SimVis**, **ComVis**, etc.) – from here: different possible paths, incl. InteractiveVisualMatlab, IVR, etc.)

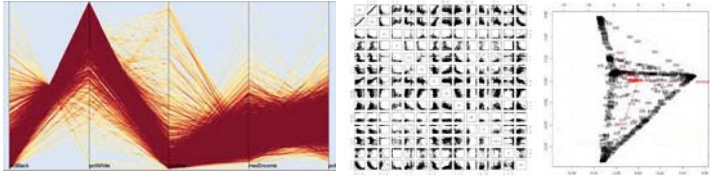
# The **Dual Analysis Framework** for **High-dimensional Data IVA**

Çağatay Turkay, Helwig Hauser  
University of Bergen



## High- vs. multi-dimensional data

- **multi-dimensional**: >3D, 4D, 6D, 12D, ..., 24D(?)



- **high-dimensional**: ..., 40D, 80D, 240D, 1200D, ...
  - std. tools for multi-dim. data vis. don't work
  - lots of statistics, etc., do not work properly, esp. when #dims. > #items

## Where?

- **Biology data** (e.g., from genomics/proteomics), **astronomy data** (e.g., spectral imaging data), **survey data** (many questions), ...

## Understanding $nD$ for (really) large $n$

### Curse of dimensionality is a problem, when $n$ large

- $nD$  distances become meaningless
- with that distances-based project methods
- statistics of wide tables don't work

### Hypothesis:

- there is valuable information in the «space of dimensions»
- the «space of dimensions» is **structured, heterogeneous**
- it's worthwhile to understand this «space of dimensions» in order to do a **better informed IVA** of the data items

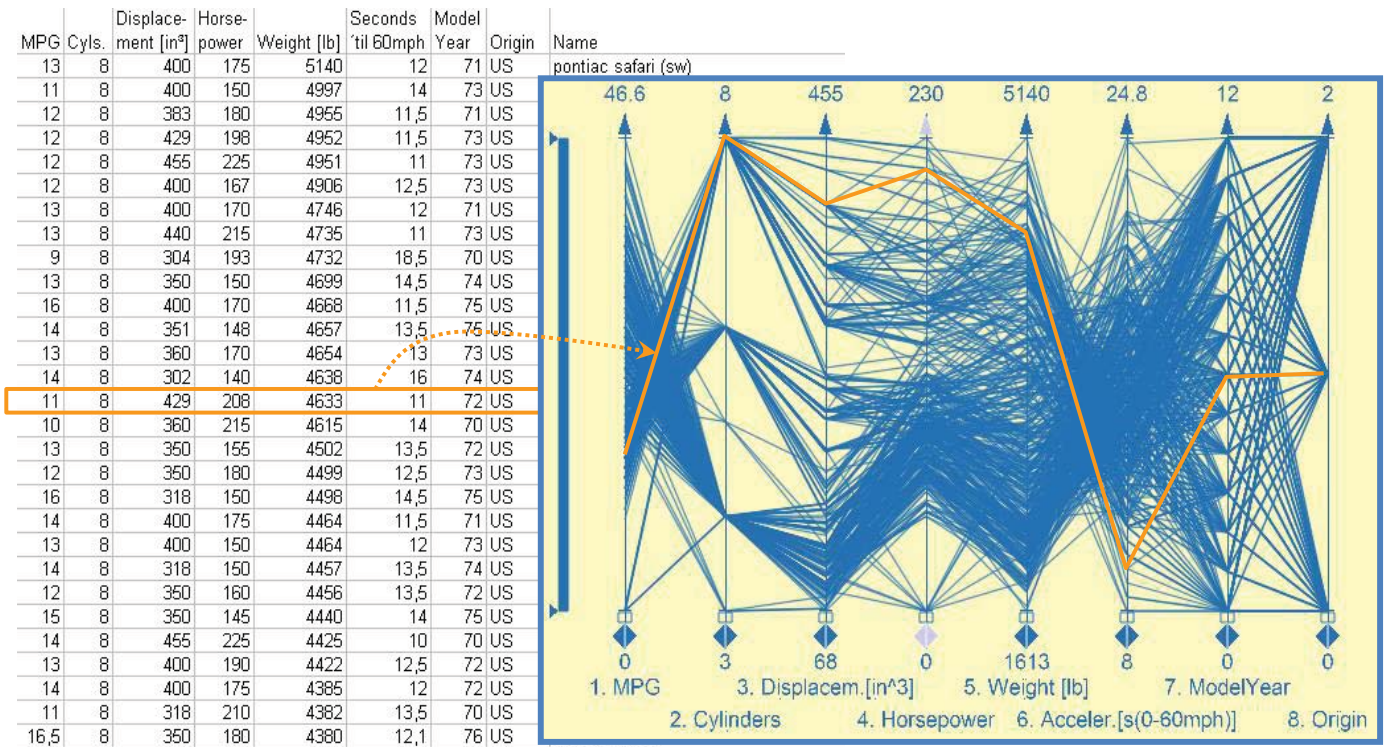
### But how to understand this «space of dimensions»?

### Can we visualize the dimensions of a dataset?



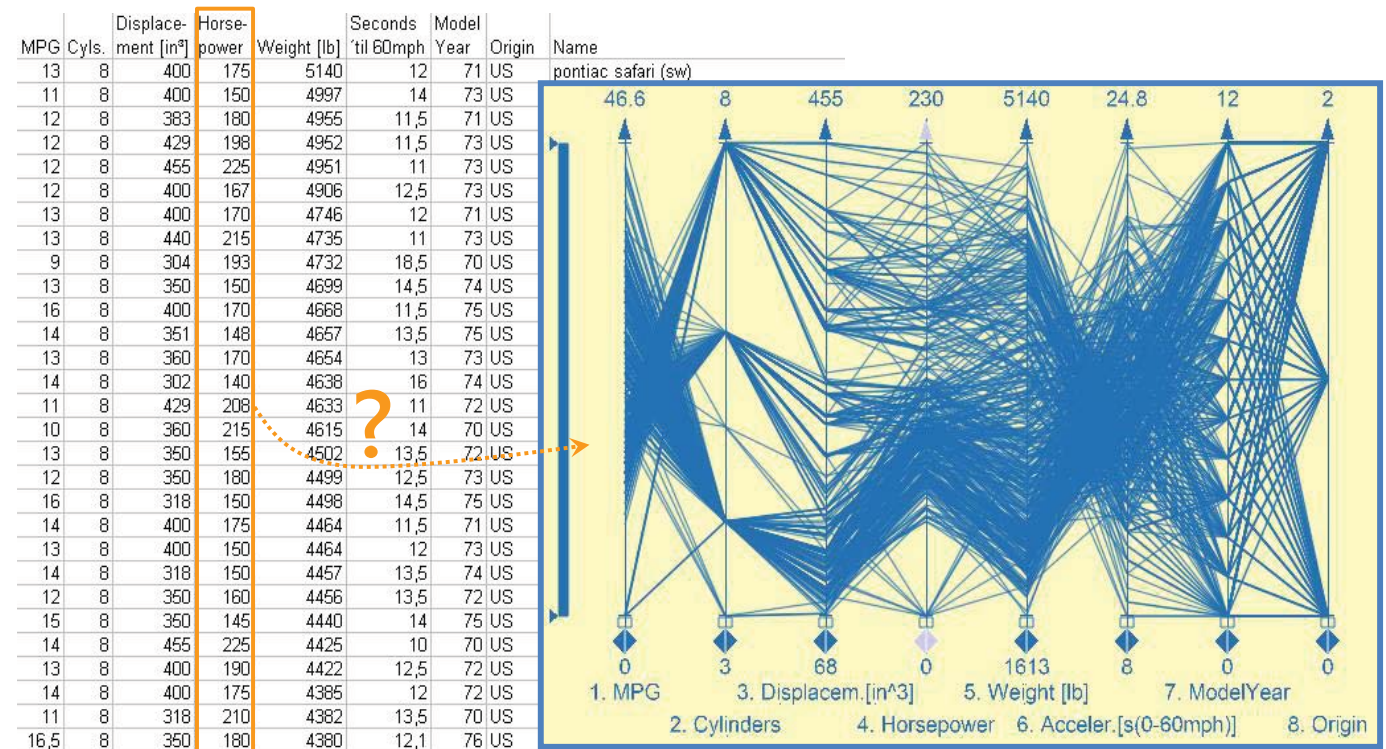
# Traditional Vis = Items Visualization

Almost all of visualization is about visualizing the (multi-dimensional) **data items**



# A new perspective: Dims. Visualization

Alternatively, and esp., when we have so many dims., we could visualize the **data dimensions** themselves!





# Naïve Approach

Transposing the data table should do it, right? :-)

Not really...

# Naïve Approach

Transposing the data table should do it, right? :-)

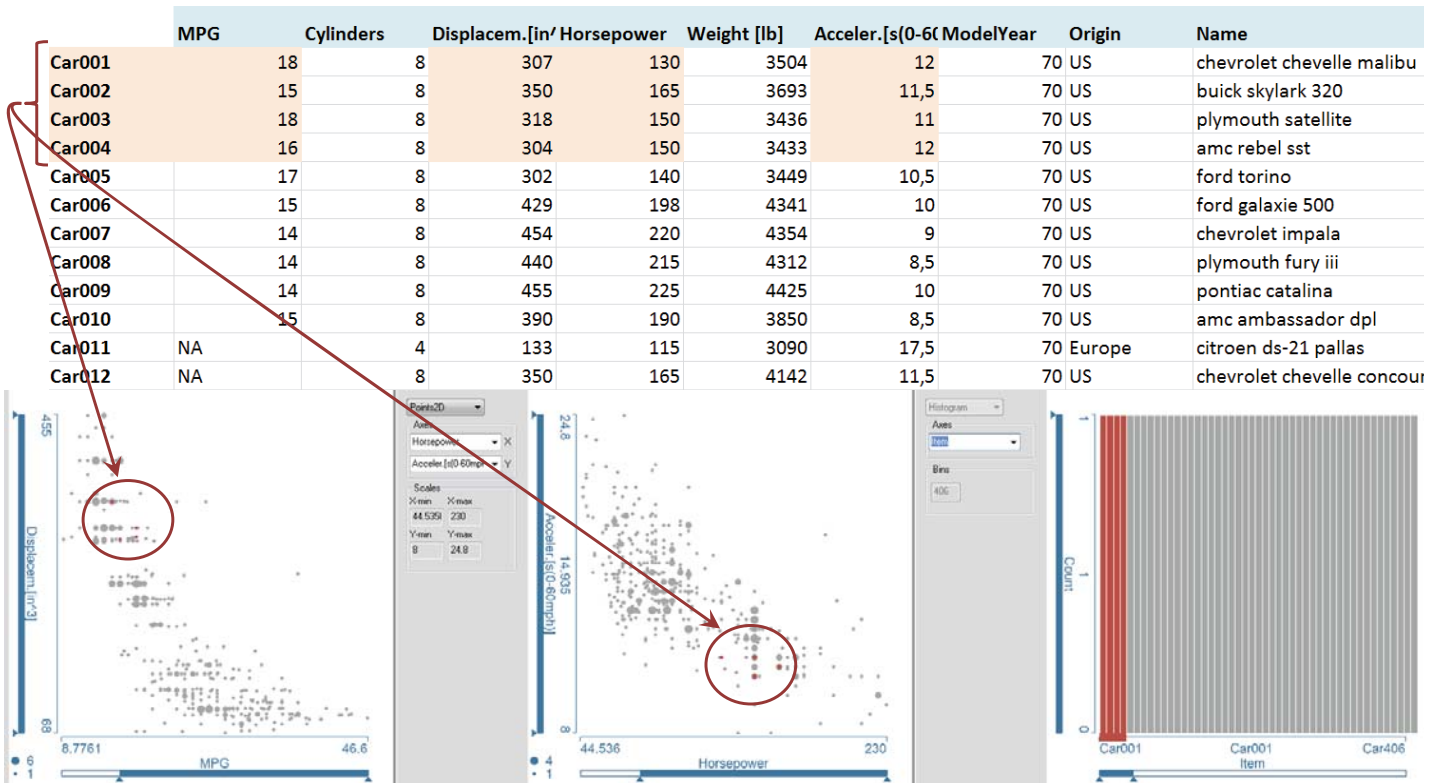
Not really...

	MPG	Cylinders	Displacem.[in'	Horsepower	Weight [lb]	Acceler.[s(0-60	ModelYear	Origin	Name
Car001		18	8	307	130	3504	12	70 US	chevrolet chevelle malibu
Car002		15	8	350	165	3693	11,5	70 US	buick skylark 320
Car003		18	8	318	150	3436	11	70 US	plymouth satellite
Car004		16	8	304	150	3433	12	70 US	amc rebel sst
Car005		17	8	302	140	3449	10,5	70 US	ford torino
Car006		15	8	429	198	4341	10	70 US	ford galaxie 500
Car007		14	8	454	220	4354	9	70 US	chevrolet impala
Car008		14	8	440	215	4312	8,5	70 US	plymouth fury iii
Car009		14	8	351	153	4425	10	70 US	pontiac catalina
Car010		15	8	390	190	3850	8,5	70 US	amc ambassador dpl
Car011	NA		8	321	115	3550	11,5	70 Europe	citroen ds-21 pallas
Car012	NA		8	360	175	4142	11,5	70 US	chevrolet chevelle concours
Car013	NA		8	351	153	4034	11	70 US	ford torino (sw)
Car014	NA		8	383	175	4166	10,5	70 US	plymouth satellite (sw)
Car015	NA		8	360	175	3850	11	70 US	amc rebel sst (sw)
Car016		15	8	383	170	3563	10	70 US	dodge challenger se
Car017		14	8	340	160	3609	8	70 US	plymouth 'cuda 340
Car018	NA		8	302	140	3353	8	70 US	ford mustang boss 302
Car019		15	8	400	150	3761	9,5	70 US	chevrolet monte carlo
Car020		14	8	455	225	3086	10	70 US	buick estate wagon (sw)
Car021		24	4	113	95	2372	15	70 Japan	toyota corona mark ii

*just for illustration.*  
**406 cars, 7 numeric dimensions**  
**(not a high-dimensional dataset!)**

# Naïve Approach

Visualizing rows (cars) from this table is standard InfoVis:



# Naïve Approach

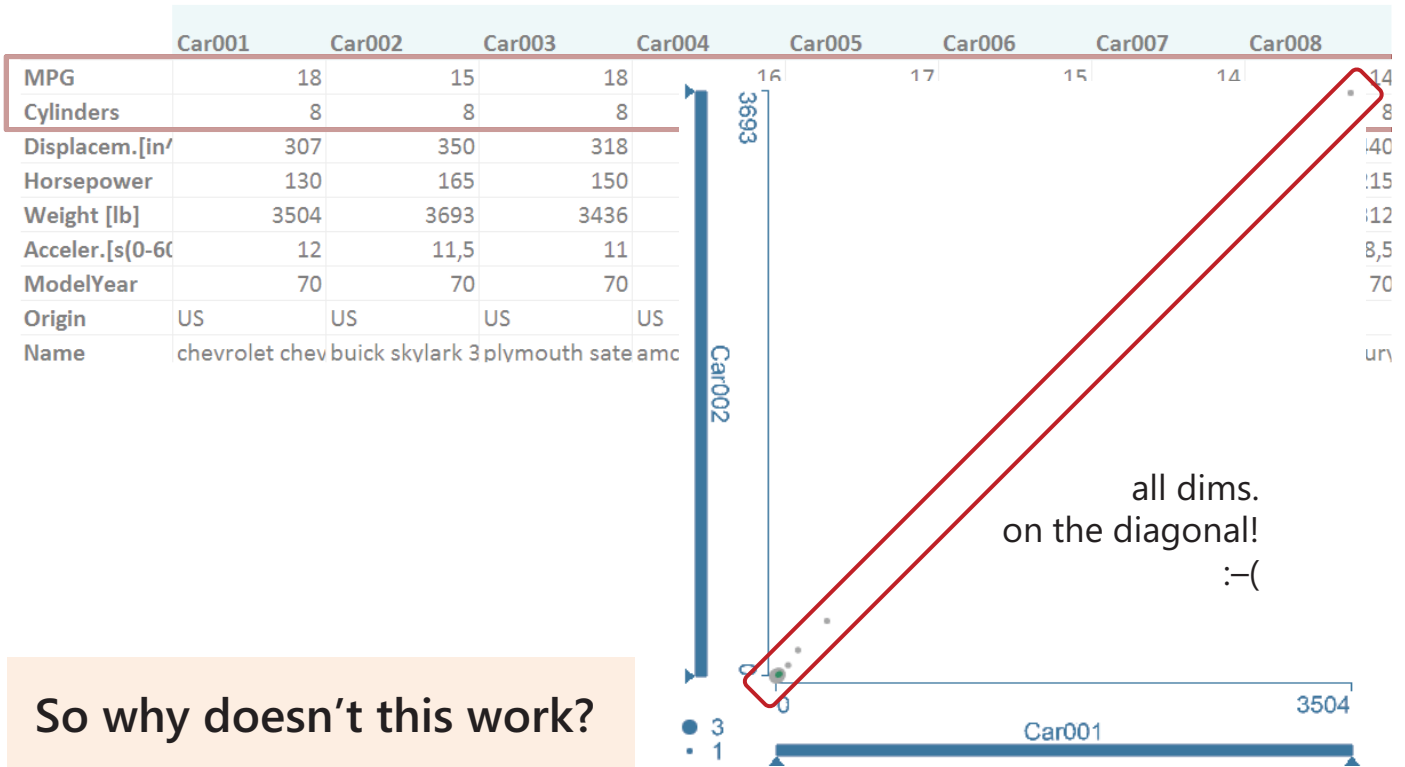
Data transposition makes the dimensions to rows:

	Car001	Car002	Car003	Car004	Car005	Car006	Car007	Car008
MPG	18	15	18	16	17	15	14	14
Cylinders	8	8	8	8	8	8	8	8
Displacem.[in³]	307	350	318	304	302	429	454	440
Horsepower	130	165	150	150	140	198	220	215
Weight [lb]	3504	3693	3436	3433	3449	4341	4354	4312
Acceler.[s(0-60)]	12	11,5	11	12	10,5	10	9	8,5
ModelYear	70	70	70	70	70	70	70	70
Origin	US	US	US	US	US	US	US	US
Name	chevrolet chev	buick skylark 3	plymouth sate	amc rebel sst	ford torino	ford galaxie 500	chevrolet impa	plymouth fury

So what about visualizing this table?

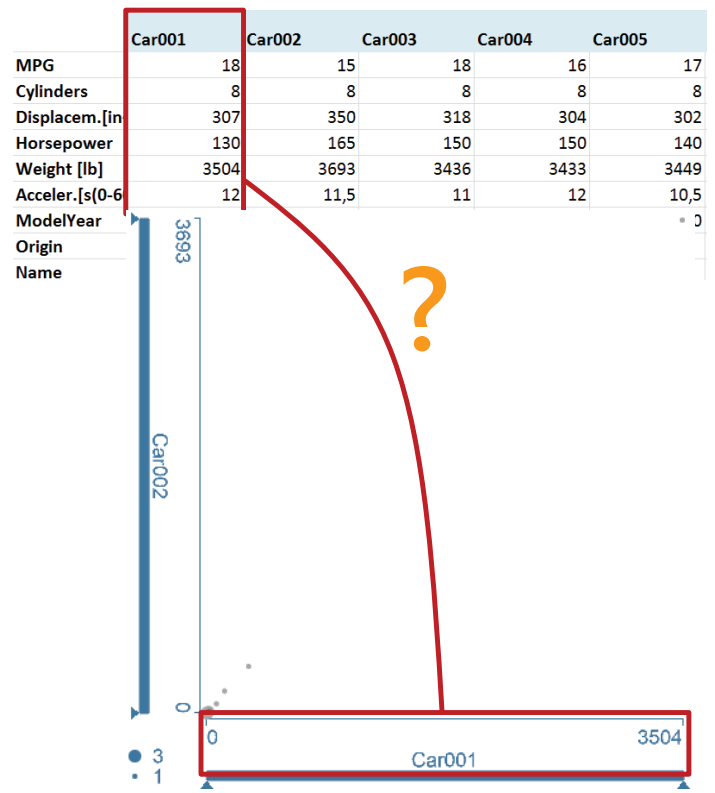
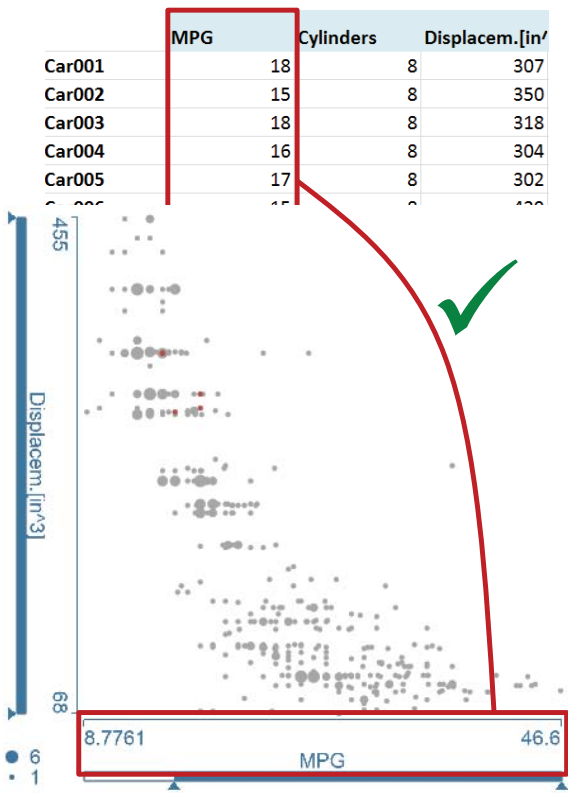
# Naïve Approach

Data transposition makes the dimensions to rows:



# Naïve Approach

No comparable values in the columns after transposition!



# Dual Analysis Framework

## What do we do, when we visualize data items?

- per data item  $\mathbf{p}_i$   
we map properties/attributes of  $\mathbf{p}_i$  to vis.-cues, f.i.,  $x$  and  $y \rightarrow$
- we see, how the  $\mathbf{p}_i$  relate to each other wrt. to their props.!

## Translating this to visualizing dimensions:

- per data dimension  $\mathbf{d}_j$   
we map properties/attributes of  $\mathbf{d}_j$  to vis.-cues, f.i.,  $x$  and  $y \rightarrow$
- we see, how the  $\mathbf{d}_j$  relate to each other wrt. to their props.!

## Expressive properties of dimensions $\mathbf{d}_j$ (selection):

- descriptive statistics, like mean and std.-der.
- measures of outlyingness

# Dual Analysis Framework

## So: constructing the properties table for dims. $\mathbf{d}_j$ :

- normalization first, then feature extraction

#Outl	40	0	31	42	44	50	35		
#Outl_high	33	0	31	40	42	25	0		
#Outl_low	7	0	0	2	2	25	35		
high_outl_th	0,698	1,013	0,735	0,638	0,748	0,700	1,008		
low_outl_th	0,076	-0,013	-0,078	0,007	0,029	0,200	0,072		
IQR	0,309	0,800	0,510	0,298	0,396	0,210	0,500		
q_3	0,532	1,000	0,605	0,457	0,570	0,548	0,750		
Med.	0,372	0,200	0,214	0,266	0,343	0,446	0,500		
q_1	0,223	0,200	0,095	0,159	0,174	0,338	0,250		
Kurt.	-0,511	-1,411	-0,811	0,541	-0,821	0,373	-1,200		
Skew.	0,457	0,506	0,694	1,034	0,506	0,230	0,021		
Std.-Dev.	0,208	0,342	0,271	0,210	0,240	0,167	0,312		
Avg.	0,39	0,50	0,33	0,32	0,39	0,45	0,54		
Max.	1,00	1,00	1,00	1,00	1,00	1,00	1,00		
Min.	0,00	0,00	0,00	0,00	0,00	0,00	0,00		
	n(MPG)	n(Cylinders)	n(Displacem.[i	n(Horsepower	n(Weight [lb])	n(Acceler.[s(0-	n(ModelYear)	Origin	Name
Car001	0,24	1,00	0,62	0,46	0,54	0,24	0,00	US	chevrolet chevelle malibu
Car002	0,16	1,00	0,73	0,65	0,59	0,21	0,00	US	buick wildcat 300
Car003	0,24	1,00	0,65	0,57	0,52	0,18	0,00	US	plymouth catalina
Car004	0,19	1,00	0,61	0,57	0,52	0,24	0,00	US	amc rebel sst
Car005	0,21	1,00	0,60	0,51	0,52	0,15	0,00	US	ford torino
Car006	0,16	1,00	0,93	0,83	0,77	0,12	0,00	US	ford galaxie 500
Car007	0,13	1,00	1,00	0,95	0,78	0,06	0,00	US	chevrolet impala
Car008	0,13	1,00	0,96	0,92	0,77	0,03	0,00	US	plymouth fury iii
Car009	0,13	1,00	1,00	0,97	0,80	0,12	0,00	US	pontiac catalina

properties table (2.)

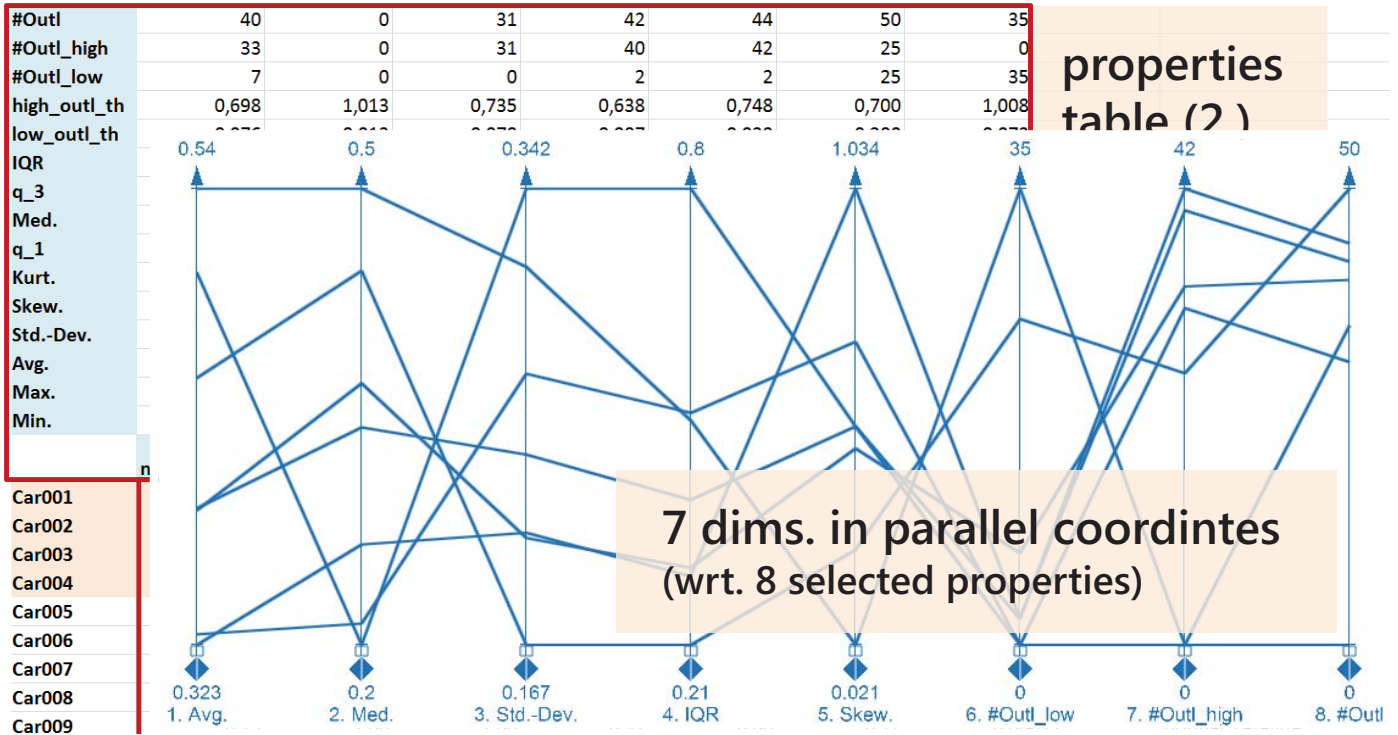
normalized data (1.)



# Dual Analysis Framework

Now we can visualize the dims.  $d_j$ !

- mapping coherent and expressive properties to vis.-cues!

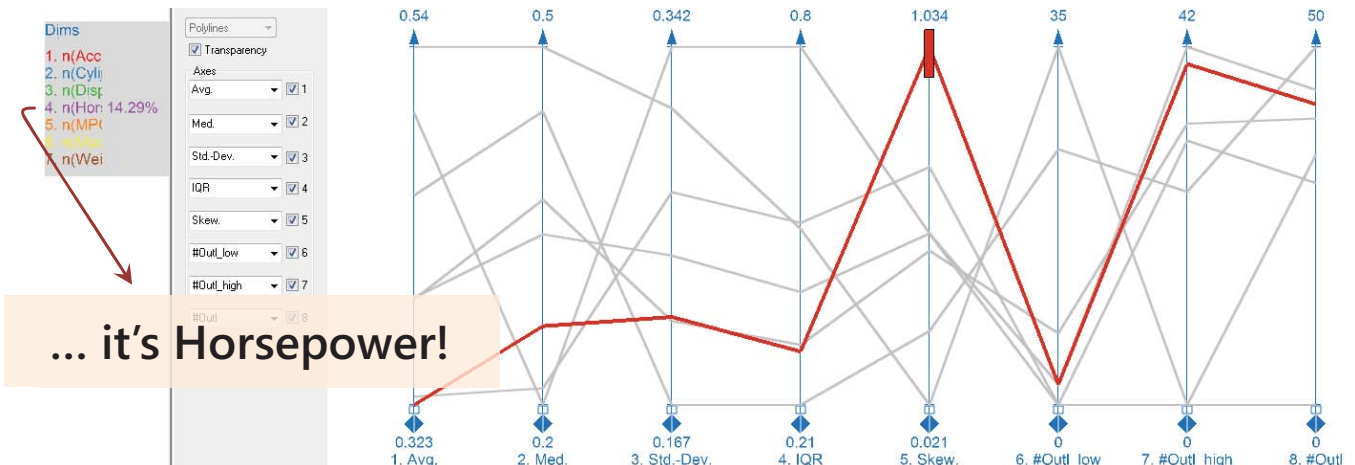


# Dual Analysis Framework

Now the dual analysis can start!

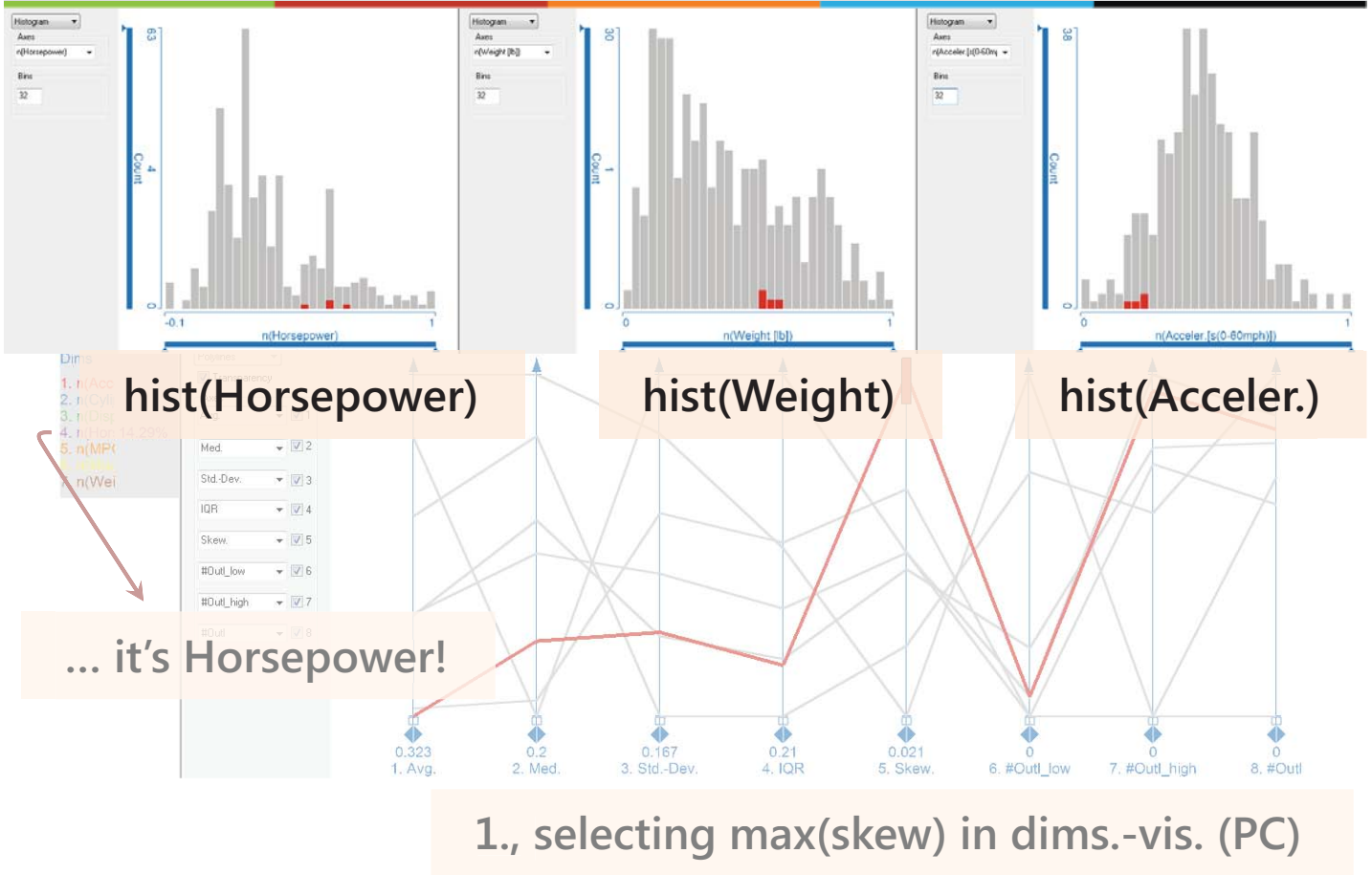
- look up informative properties in the dims.-vis.
- do related items-visualization, accordingly

Example 1: exploring the most skewed dimension



1., selecting max(skew) in dims.-vis. (PC)

# Dual Analysis Framework

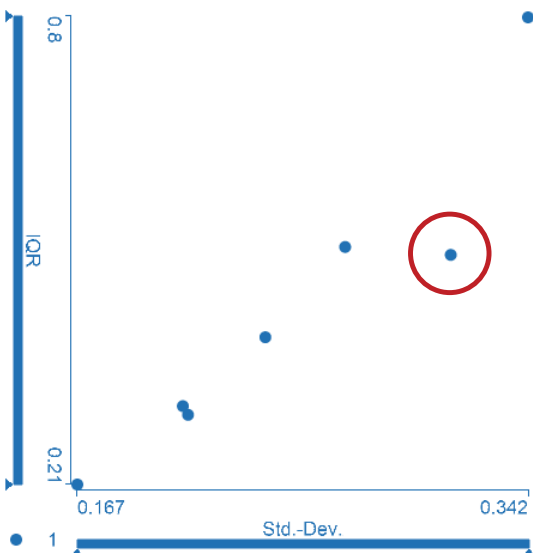


# Dual Analysis Framework

Now the dual analysis can start!

- look up informative properties in the dims.-vis.
- do related items-visualization, accordingly

Example 2: comparing Gaussian & ranking-based stats.



1., seeing that both measures for the spread (std.-dev. vs. IQR) agree for all but one dim.

2., selecting it (not shown) reveals: it's ModelYear, a discrete data dimension...

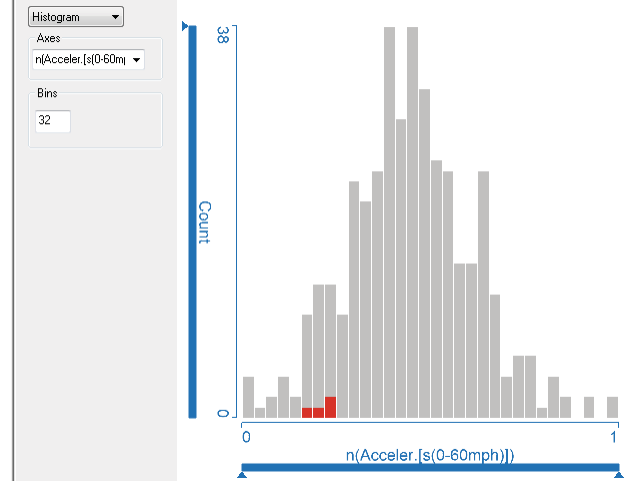
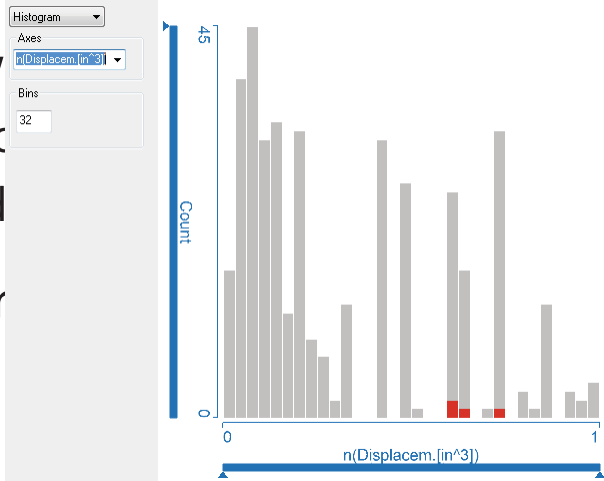
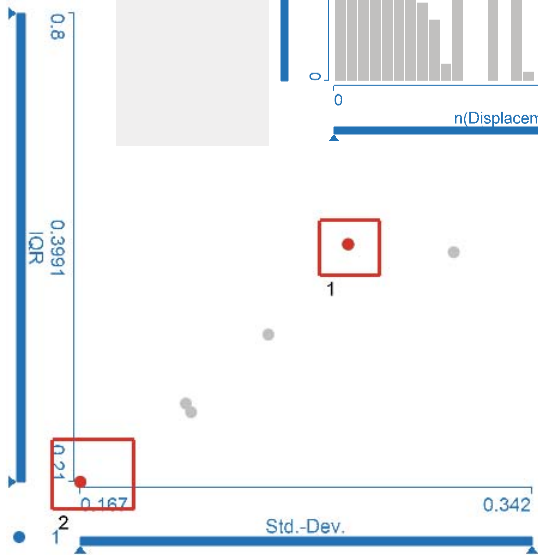
# Dual Analysis Framework

Now

– look up

– do related

Example



next:  
comparing a low-spread (Accel.)  
vs. a high-spread dim. (Displacem.)

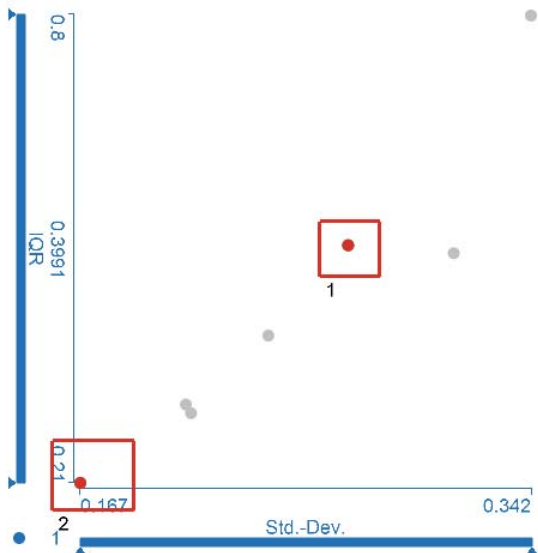
... the top-right dim. – max. spread –  
is Cylinders – basically categorical...

# Dual Analysis Framework

Now the dual analysis can start!

- look up informative properties in the dims.-vis.
- do related items-visualization, accordingly

Example 2: comparing Gaussian & ranking-based stats.



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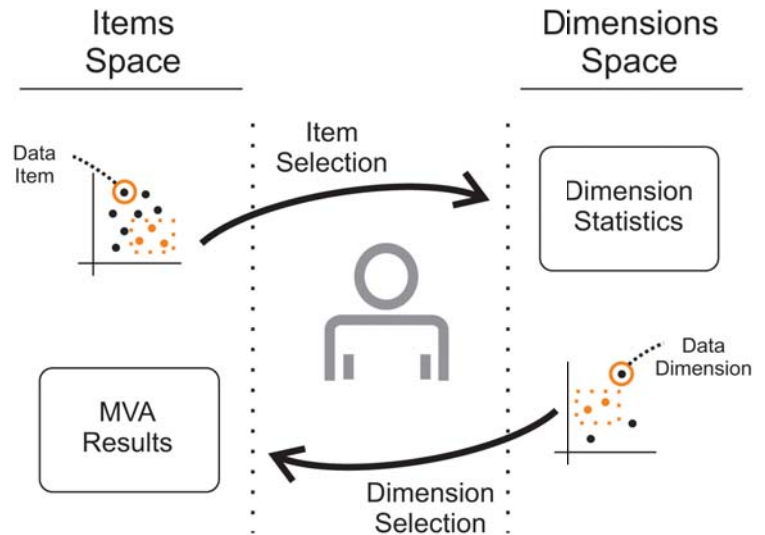
# Dual Analysis Framework

Quickly, we explore the dims. according to their props.

- hundreds or thousands of dims. → no problem! :-)
- dozens of properties → std. InfoVis is fine!

The Dual Analysis emerges through iteration:

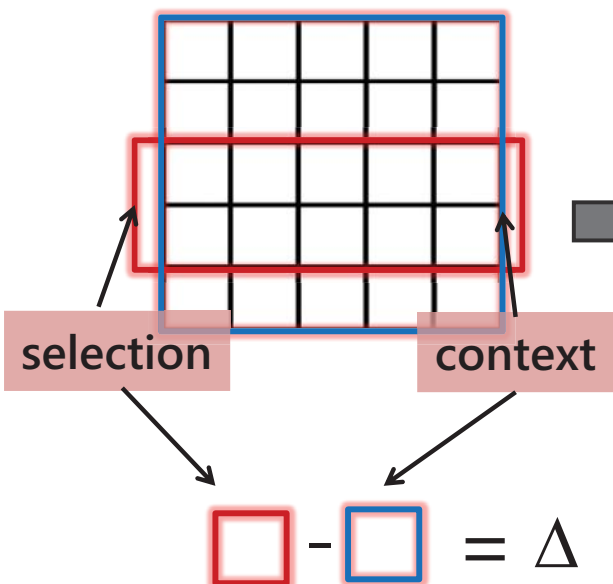
- one key tool:  
the difference view



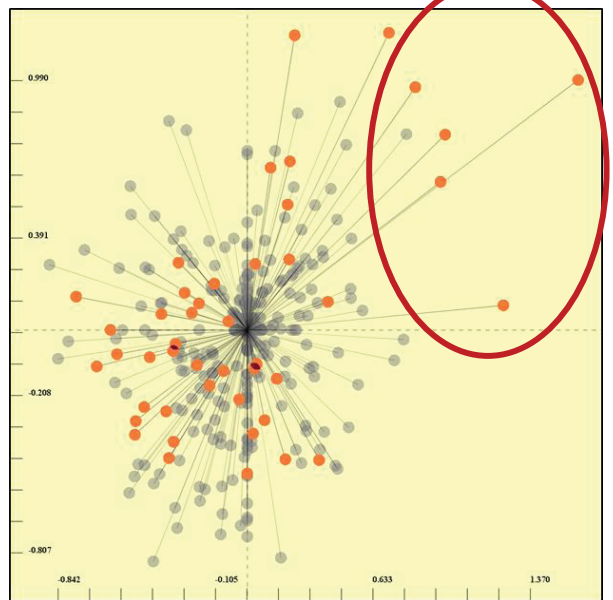
# Dual Analysis Framework

Working with the difference view

Higher values for the selection



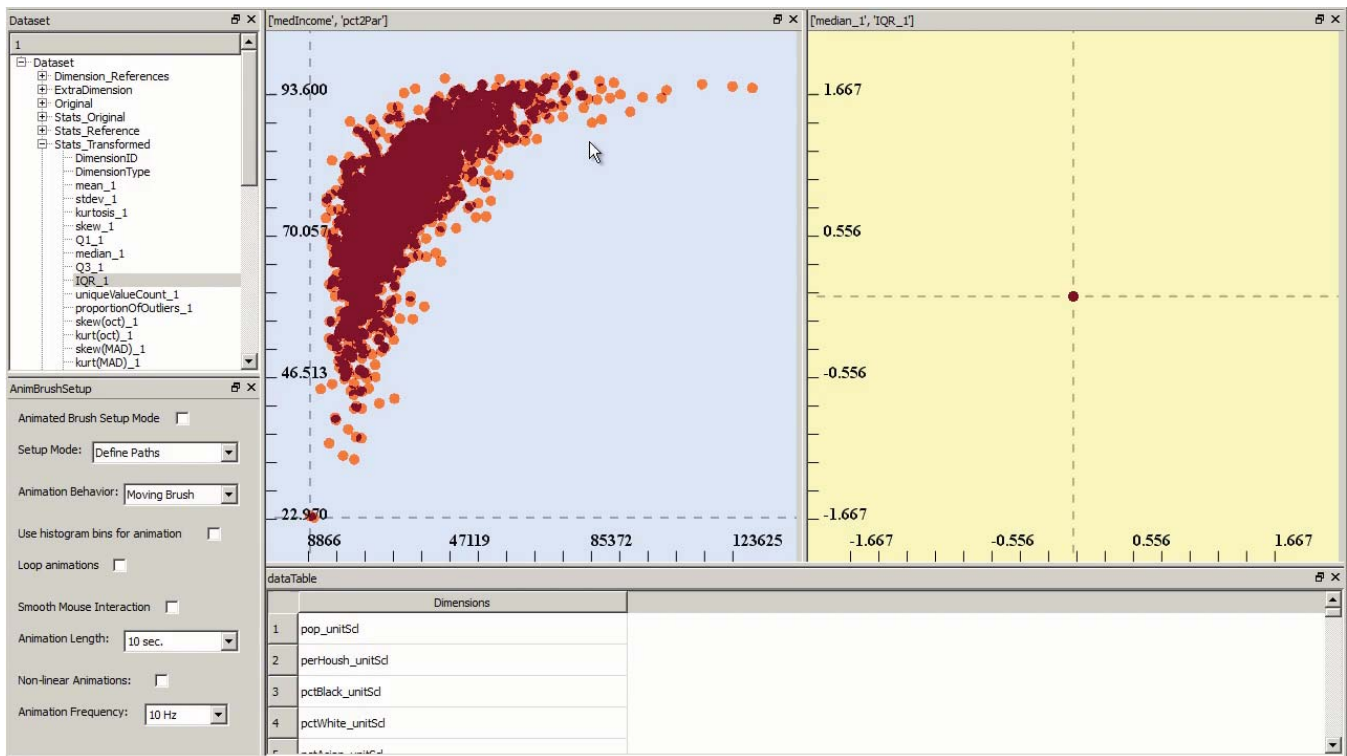
Change in IQR values



Change in med values



## Difference View in action:



# Dual Analysis Framework

## More in the thesis / papers of Çağatay Turkay *et al.*

C. Turkay, P. Filzmoser, and H. Hauser. **Brushing Dimensions-A Dual Visual Analysis Model for High-Dimensional Data.** *IEEE Transactions on Visualization and Computer Graphics*, 17(12):2591-2599, 2011.

C. Turkay, A. Lundervold, A.J. Lundervold, and H. Hauser. **Representative Factor Generation for the Interactive Visual Analysis of High-Dimensional Data.** *IEEE Transactions on Visualization and Computer Graphics*, 18(12):2621-2630, 2012.

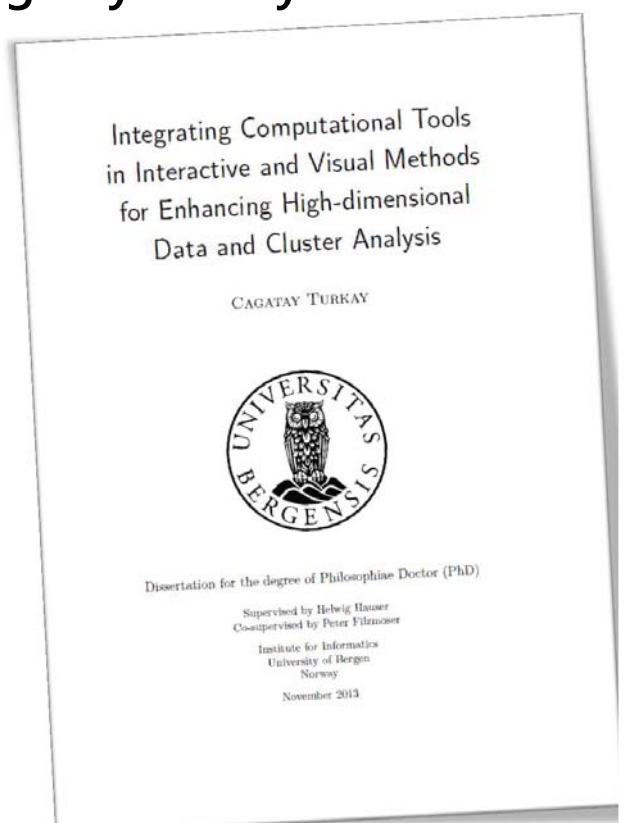
C. Turkay, P. Angelelli, P. Filzmoser, and H. Hauser. **Outlier Dimensions – Outlier Aware Analysis of High-dimensional Data.** In submission to: *IEEE Transactions on Visualization and Computer Graphics*, 2013.

C. Turkay and H. Hauser. **Optimizing Processes in Visual Analytics to Meet the Three Human Time Constants.** In submission to: *Computers and Graphics*, 2013.

C. Turkay, A. Lundervold, A.J. Lundervold, and H. Hauser. **Hypothesis Generation by Interactive Visual Exploration of Heterogeneous Medical Data.** *Human-Computer Interaction and Knowledge Discovery in Complex, Unstructured, Big Data. Lecture Notes in Computer Science*, Volume 7947:1-12, 2013.

C. Turkay, A. Lex, M. Streit, H.P. Pfister, and H. Hauser. **Characterizing Cancer Subtypes using the Dual Analysis Approach in Caleydo.** In submission to: *IEEE Computer Graphics and Applications*, 2013.

C. Turkay, J. Parulek, N. Reuter, and H. Hauser. **Interactive Visual Analysis of Temporal Cluster Structures.** *Computer Graphics Forum*, 30(3):711-720, 2011.



# Acknowledgements



You!

We'd like to hire  
➤ 1 PostDoc

Luis  
Gustavo!

Collaborators:

H. Doleisch, R. Fuchs/Bürger,  
J. Kehrer, Ç. Turkay, Z. Konyha,  
Kr. Matković, P. Filzmoser,  
*et al.*

UNIVERSITY OF BERGEN 

### Upcoming Job Opportunities in Visualization at the University of Bergen

The visualization research group at the University of Bergen's Department of Informatics, Norway (UIB), is preparing the announcement of two open positions. We invite all potentially interested applicants to contact us directly for further details.

**1 PhD Fellowship (4 years):**  
*We are looking for a highly motivated individual with interest in the visualization of medical data. Suitable applicants should have a background in visualization, human-computer interaction, and/or computer graphics and very good programming skills. Since eligible candidates are required to have completed their Master's degree prior to the upcoming job announcement, we ask all interested candidates to contact us as soon as possible.*  
Contact: Prof. Stefan Bruckner ([stefan.bruckner@uib.no](mailto:stefan.bruckner@uib.no))

**1 Postdoctoral Fellowship (4 years):**  
*We are looking for a promising scholar to fill a postdoctoral fellowship in visualization. This strategic position is not associated with a specific research project, but meant to strengthen the core visualization research activities in Bergen – considerable flexibility in terms of filling this appointment is envisioned. Applicants should have a completed PhD degree in visualization or a closely related subject, a strong publication record, a strong interest in high-quality research and also substantial interest in teaching of visualization and related topics.*  
Contact: Prof. Helwig Hauser ([helwig.hauser@uib.no](mailto:helwig.hauser@uib.no))

**The University of Bergen**  
The University of Bergen, Norway (UIB), has approximately 14,500 enrolled students and 3,200 faculty and staff. Six faculties cover most of the traditional university disciplines. Within the faculties there are 40 different specialized departments, multi-disciplinary research centers, and institutes. The University is engaged in the European Union's Framework programs for research and technological development and has been designated as a European Research Infrastructure and a Research Training Site in several scientific fields. Since 1997 more than 500 European researchers (professors, senior researchers, post docs and PhD candidates) have visited Bergen on EU grants, making UIB one of the most international universities, setting out to attract both established and junior scientists to contribute to research teams and work in multidisciplinary research groups. Further information: <http://www.uib.no/en>

**The Visualization Group**  
The Department of informatics at UIB is a dynamic international environment. The visualization research group was established in 2007 and focuses on new solutions for the effective and efficient visualization of large and complex data from measurements (e.g., from medical imaging or from seismic/sonar sensors), computational simulation (e.g., from computational fluid dynamics), or from analytic modeling (e.g., in the form of differential equations) for the purpose of data exploration, analysis, and presentation. Despite being a still relatively young group, the recent ten-year evaluation of all 62 informatics research groups in Norway conducted by an international evaluation panel on behalf of Norway's Research Council, found that the group's "[...] accomplishments made so far are excellent." and concluded with an overall assessment of "very good to excellent". Further information: <http://www.uib.no/vis>

**The City of Bergen**  
Bergen is Norway's second largest city with over 260,000 inhabitants and is located in the county of Hordaland on the south-western coast of Norway, known as the "gateway to the fjords", Bergen is surrounded by spectacular scenery. As one of the offices of the Hanseatic League, Bergen was for several hundred years the center of prosperous trade between Norway and the rest of Europe. Today, Bergen is a lively and vibrant city with an international flair. Every semester the city with its university and colleges are proud and enthusiastic to welcome students from all over the world. Bergen is one of the most popular student cities in Scandinavia with 50,000 students in many different educational institutions. Its international atmosphere, together with the fact that Norway has been voted #1 in standard of living by the UNDP's Human Development Index for several years, make Bergen a very attractive place for life and study. Further information: <http://www.visitbergen.com/en>

